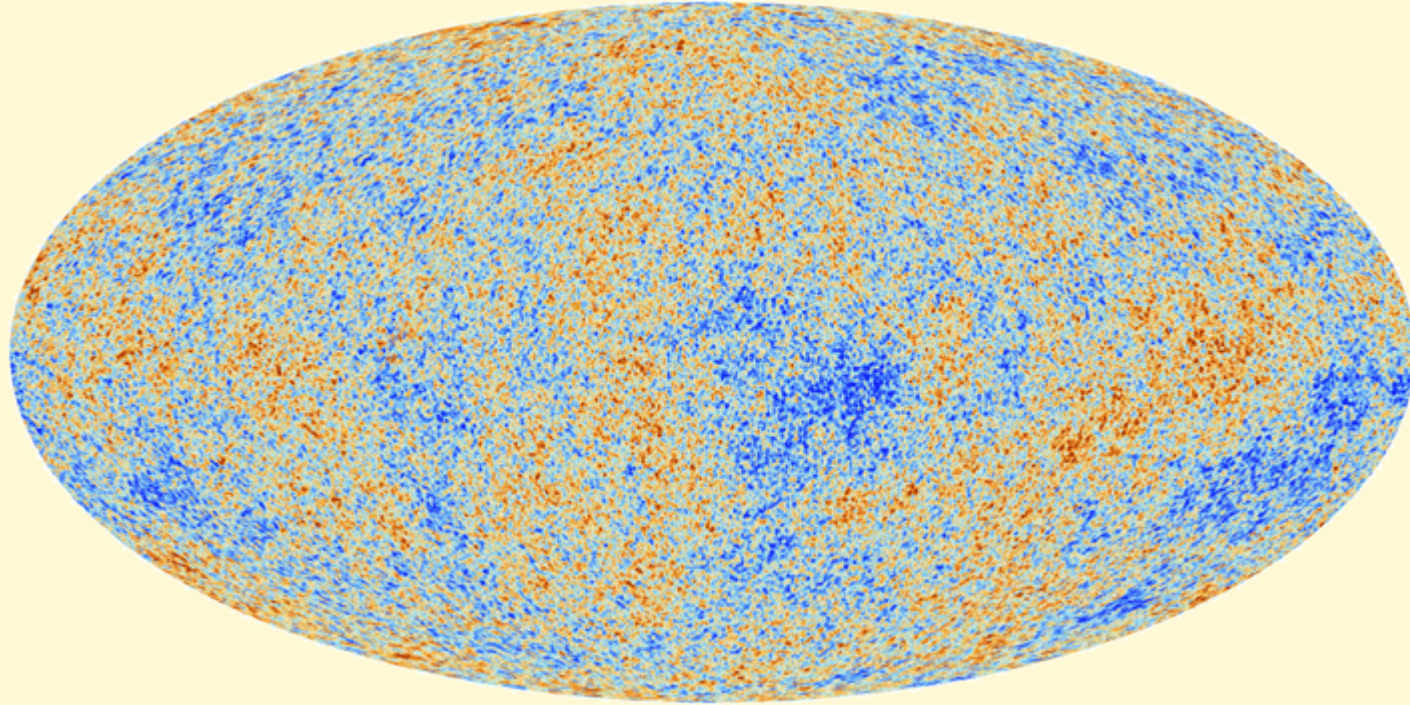


Het vroege en late heeral

It's all about energy densities

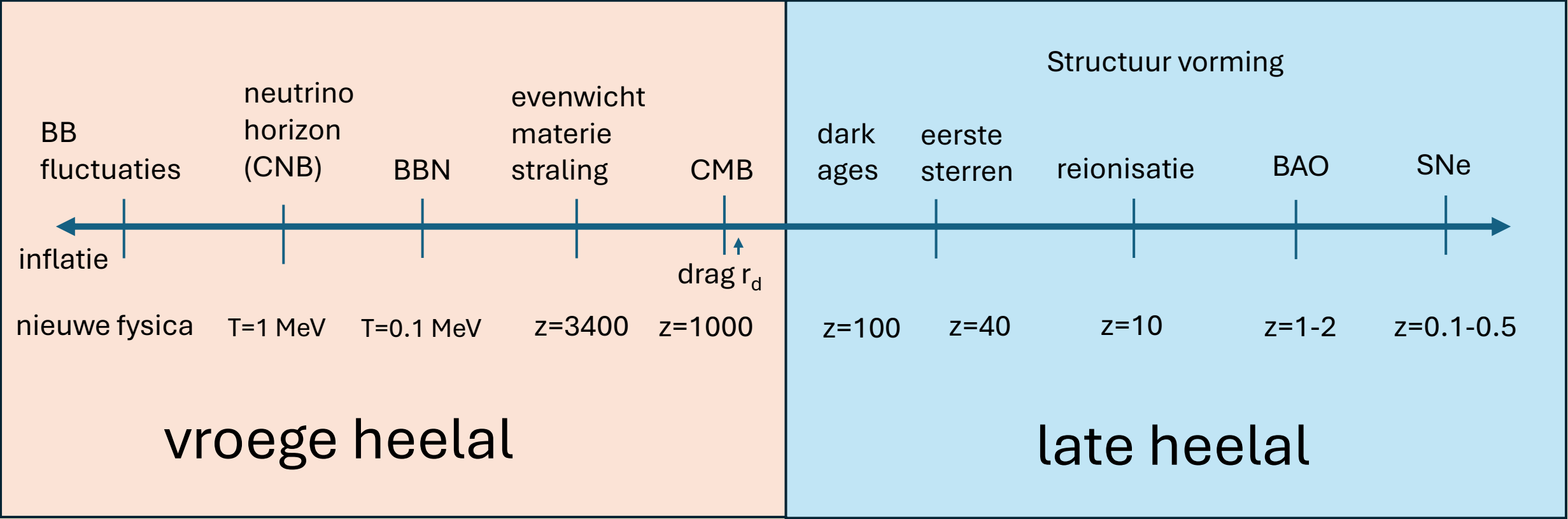


Processen in het vroege heelal laten hun sporen na in het late heelal



De 'baby foto' van het heelal – temperatuur uit de microgolf achtergrond straling door de Planck satelliet

Tijdlijn evolutie (definitie vroeg/laat)



Verhaal van de materie (en in het begin ook van de straling)

Energiedichtheden

Fysisch meten we ρ_i of $\Omega_i h^2$

maar voor de **evolutie** willen we Ω_i

De **Hubble constante** verbindt beide

relativistisch	Niet relativistisch
fotonen	baryonen
neutrino's	(koude) donkere materie

$$\Omega_{rel} = \Omega_\gamma + \Omega_\nu$$

$$\Omega_m = \Omega_b + \Omega_c$$

$$(\Omega_m = \Omega_{bar} + \Omega_{cdm})$$

$$H(z) = H_0 E(z)$$

$$E(z) = \sqrt{\Omega_{rel,0}(1+z)^4 + \Omega_{m,0}(1+z)^3 + \Omega_{\Lambda,0}}$$

In het vroege heelal vnl. Ω_{rel} en Ω_m

In het late heelal vnl. Ω_m en Ω_Λ

Roodverschuiving: $z = \frac{\lambda_0}{\lambda(t)} - 1$ $\Omega_{rad} = \Omega_{rel}$ (radiation (straling) versus relativistisch, hier $\Omega_{rad} = \Omega_\gamma$)

ρ_i fysische energiedichtheid

Ω_i relatieve energiedichtheid

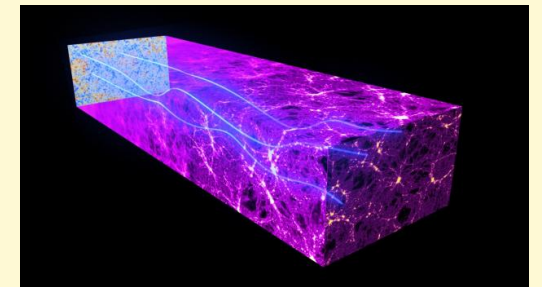
$$\Omega_i = \frac{\rho_i(t)}{\rho_c} = \frac{8\pi G \rho_i(t)}{3H_0^2}$$

$$\Omega_i h^2 = \frac{8\pi G \rho_i(t)}{30000}$$

$$h = \frac{H_0}{100}$$

We kennen vaak de fysische energie dichtheden, maar niet de relatieve omdat we H_0 niet goed kennen

Isatroop en homogeen & vlak heelal (gemiddeld geen kromming)



$$\Omega_{rel} + \Omega_m + \Omega_\Lambda = 1$$

Gewone materie: baryonen, dwz protonen en neutronen (samenstelsel van 3 quarks):

- Hoeveel is er?
- Waar komen vandaan?
- Wat maken ze mee?

relative baryon density

$$\Omega_b = \frac{\rho_b(t)}{\rho_c} = \frac{8\pi G \rho_b(t)}{3H_0^2}$$

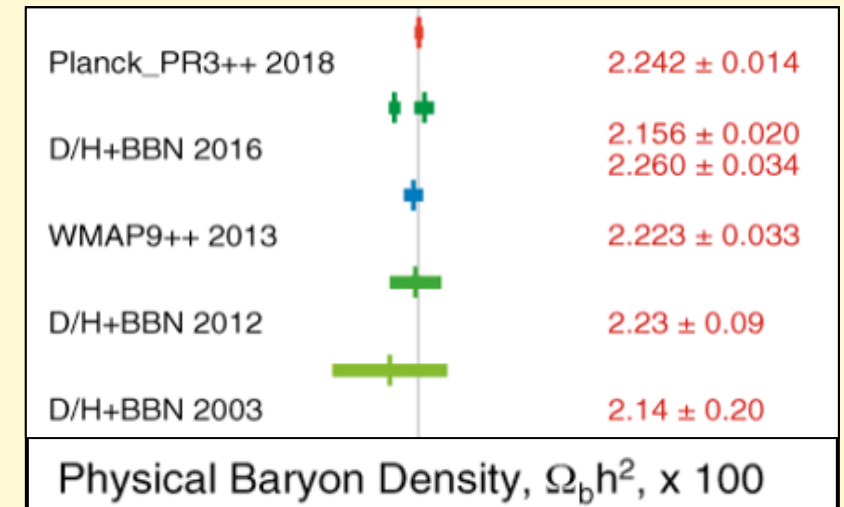
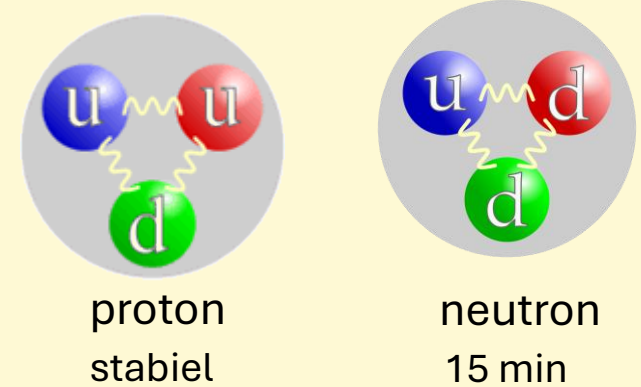
physical baryon density

$$\Omega_b h^2 = \frac{8\pi G \rho_b(t)}{30000}$$

- Hoe weten we hoeveel er is?
 - BBN theorie
 - D/H meting oerwolken rond quasars
 - CMB theorie

$$m_p c^2 = 938 \text{ MeV rust massa proton}$$

$$n_b \propto \frac{\Omega_{b,0} h^2}{m_p c^2} \approx 2.3 \cdot 10^{-7} \text{ cm}^{-3}$$



[LAMBDA - Baryonic Density](#)

[Bartelmann-7.pdf](#)

Fotonen

relative photon density

$$\Omega_{\gamma,0} = \frac{\rho_{\gamma}(t_0)}{\rho_c} = \frac{8\pi G \rho_{\gamma}(t_0)}{3H_0^2}$$

physical photon density

$$\Omega_{\gamma,0} h^2 = \frac{8\pi G \rho_{\gamma}(t_0)}{30000}$$

$$\rho_{\gamma} \sim T_{\gamma}^4$$

$$\rho_{\gamma} \sim n_{\gamma} T_{\gamma}$$

$$T_{\gamma} \sim (z + 1)$$

Stefan-Boltzmann

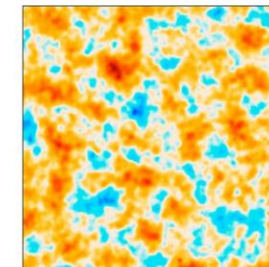
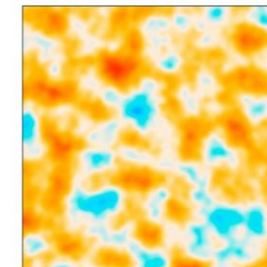
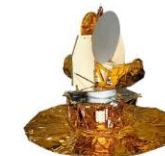
$$n_{\gamma} \sim T_{\gamma}^3$$

$$n_{\gamma} = 410 \text{ cm}^{-3} \left(\frac{T_{\gamma}}{2.725\text{K}} \right)^3$$

Waar komen de fotonen van de achtergrond straling vandaan?

[Radiation Energy Density](#)

[The Cosmic Microwave Background Radiation - E. Gawiser & J. Silk](#)

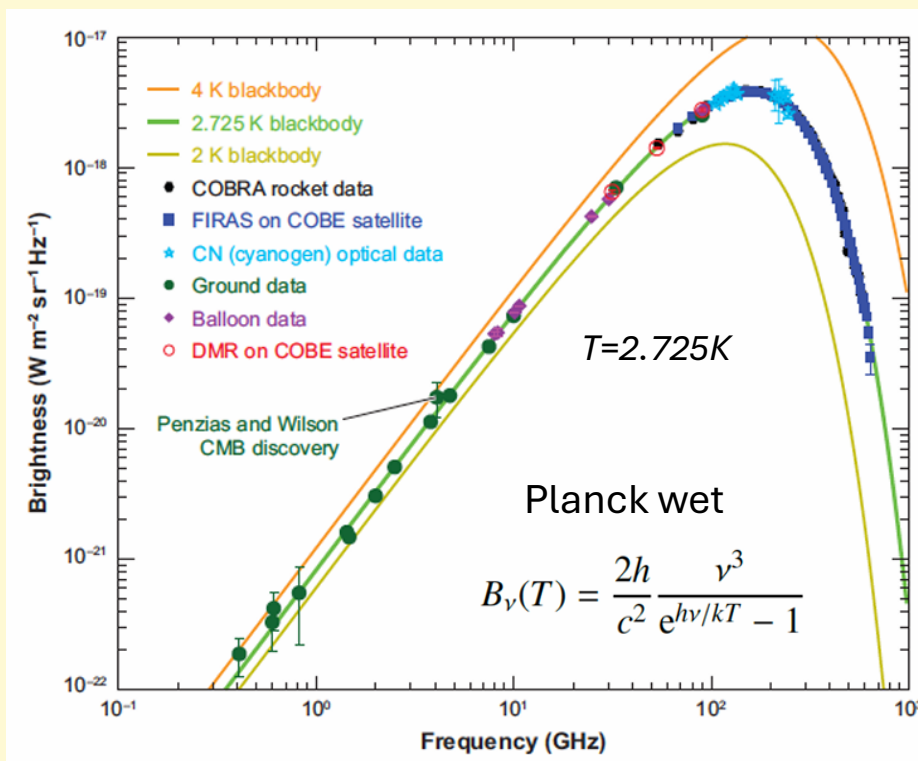


COBE

WMAP

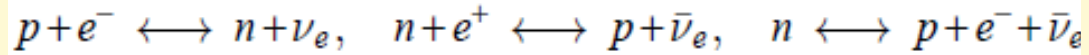
Planck

Wat meet COBE?

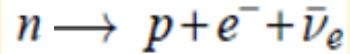


Zwakke interactie ont koppeling & CNB

Voor ont koppeling evenwicht:



Na ont koppeling alleen:



Gevolgen ont koppeling:

Neutrino's ont koppeld $\rightarrow$ CvB
(cosmic neutrino background)

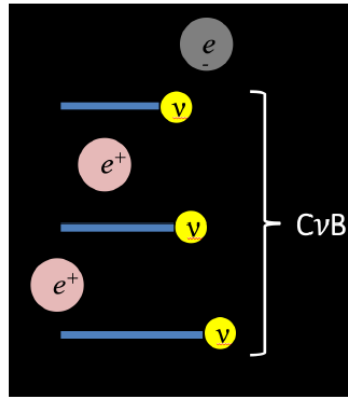
Vaste neutron/proton verhouding

$$\left(\frac{n}{p}\right)_{eq} \propto \exp\left(-\frac{\Delta mc^2}{kT}\right) \approx \frac{1}{6} \rightarrow \frac{1}{7}$$

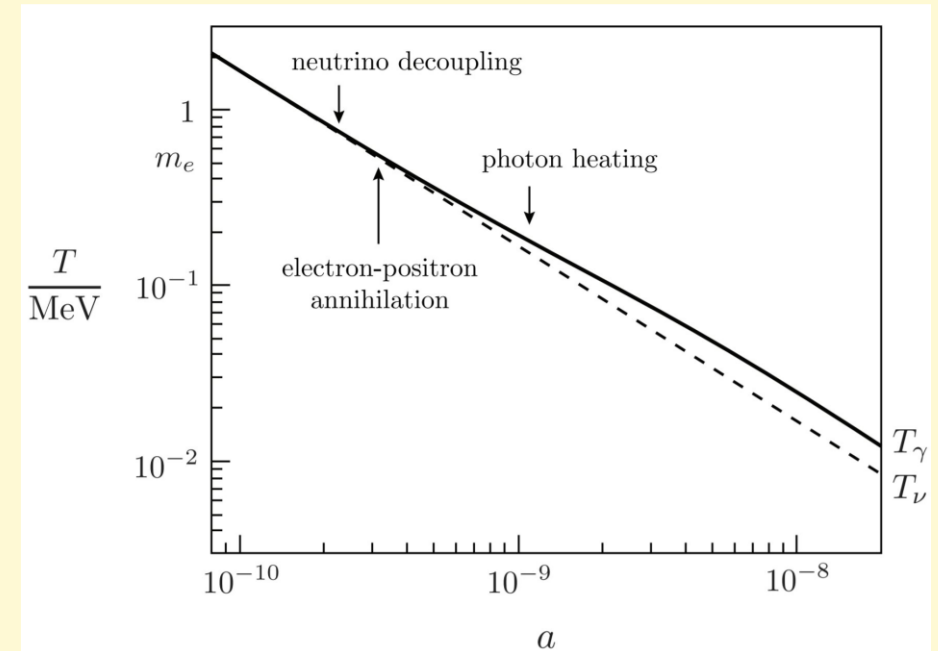
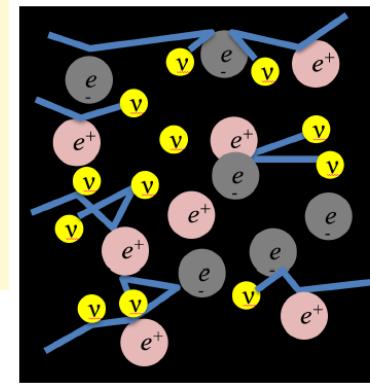
e^+, e^- annihilatie bij $kT \sim 0.8$ MeV
 $\rightarrow$ boost foton temperatuur

$$T_\nu = T_\gamma \longrightarrow T_\nu = \left(\frac{4}{11}\right)^{\frac{1}{3}} T_\gamma$$

$$\rho_\nu = N_{eff} \frac{7}{8} \left(\frac{4}{11}\right)^{\frac{4}{3}} \rho_\gamma \quad N_{eff} \sim 3$$

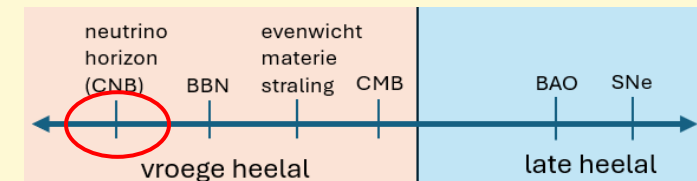


Neutrinos
"free-stream"
to infinity.



Relativistisch heelal
 $T(t) \sim 10^{10} \text{ K } (t/1\text{sec})^{-1/2}$
 $kT(t) \sim 1 \text{ MeV } (t/1\text{sec})^{-1/2}$

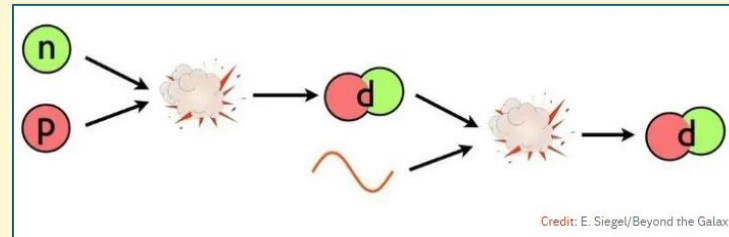
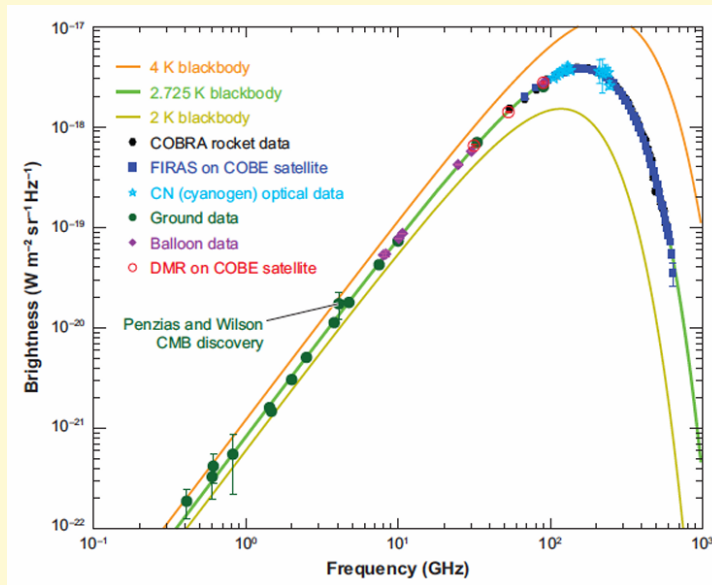
Ont koppeling bij
 $t \sim 1\text{sec}$
 $kT \sim 1 \text{ MeV}$



BBN - Deuterium bottleneck

$\Delta_D = 2.23 \text{ MeV}$ bindings energie deuterium

$$\eta = \frac{n_b}{n_\gamma} = 6.1 \cdot 10^{-10} \text{ aantal baryonen t.o.v. fotonen}$$

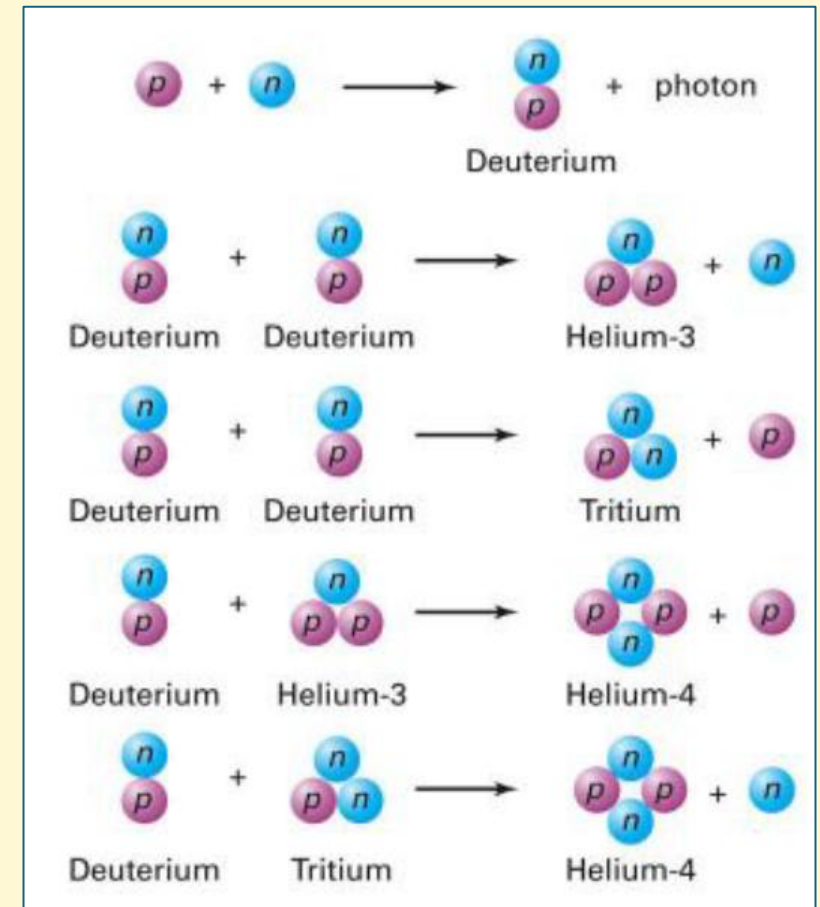


hoge energie staart



Bij $T \sim 0.1 \text{ MeV}$ $\eta^{-1} \exp\left(-\frac{\Delta_D}{kT}\right) < 1$

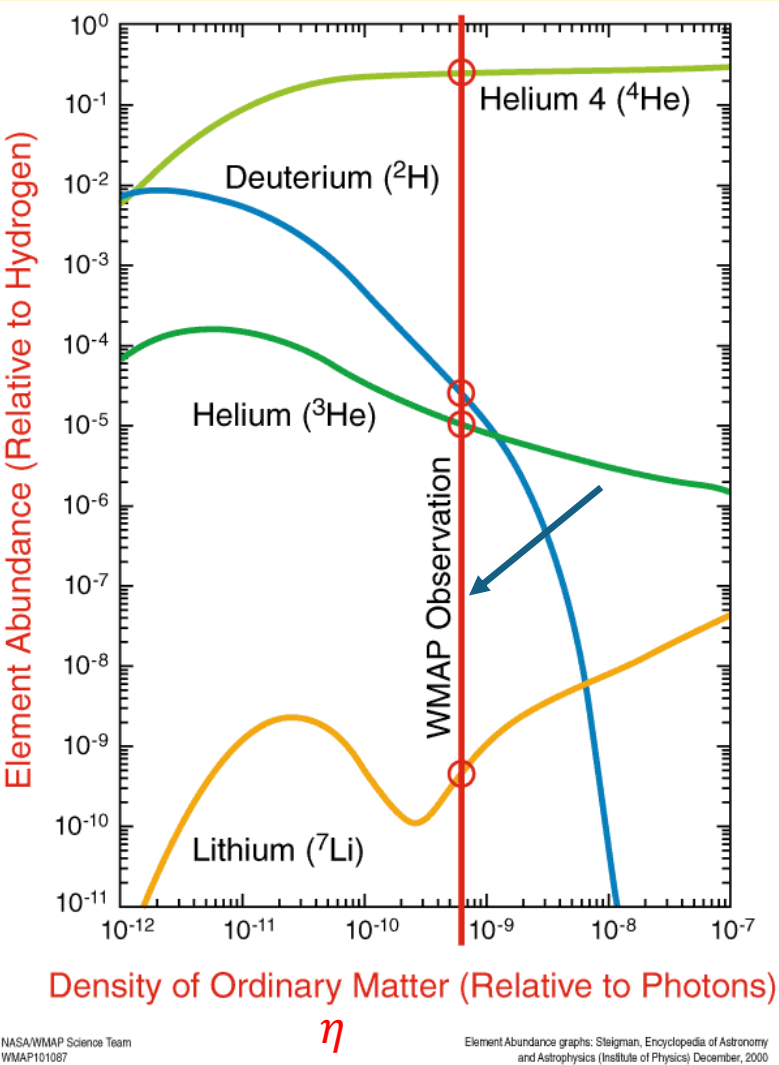
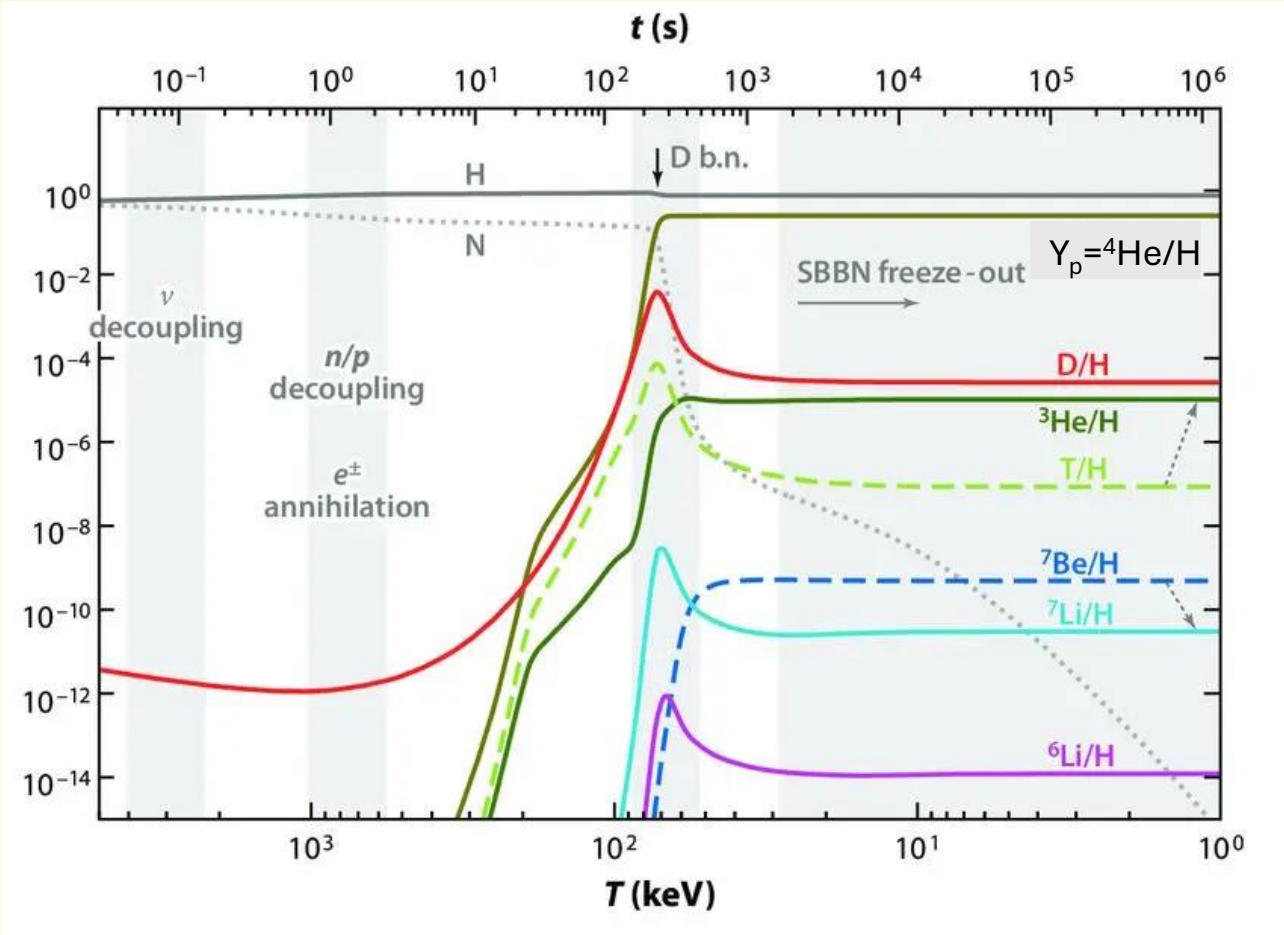
$kT(t) \sim 1 \text{ MeV} (t/1 \text{ sec})^{-1/2} \longrightarrow t \sim 100 \text{ sec}$



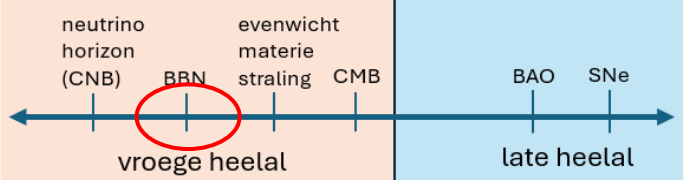
Na deuterium gaat vervolg snel en worden meeste neutronen weggevangen

BBN - Baryon afhankelijkheid

deuterium vorming is erg gevoelig voor η en dus ook voor $\frac{\Omega_{b,0}}{\Omega_{\gamma,0}}$

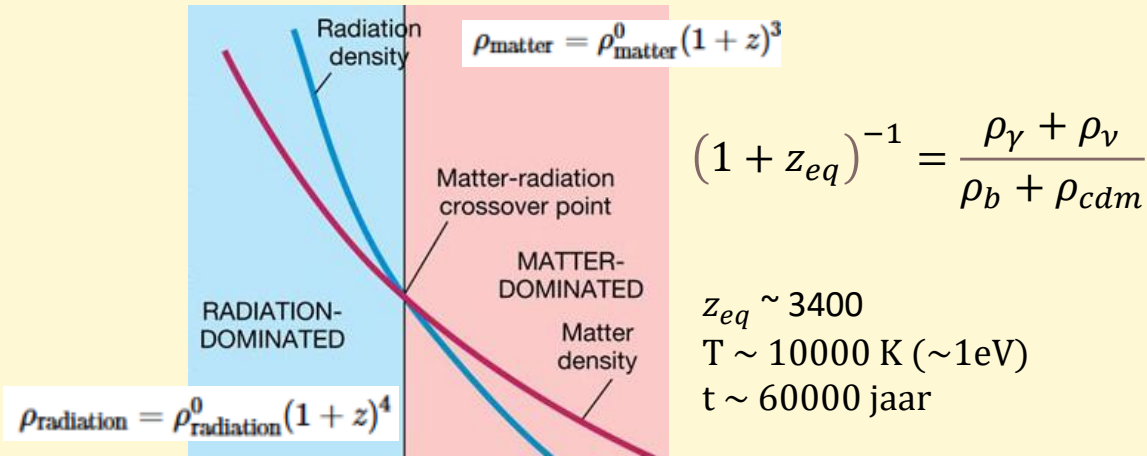


NASA/WMAP Science Team WMAP101087 Element Abundance graphs: Steigman, Encyclopedia of Astronomy and Astrophysics (Institute of Physics) December, 2000



Uitdijing meten (m.b.v. de geluidshorizon)

Uitdijing (overgang naar materie dominant)

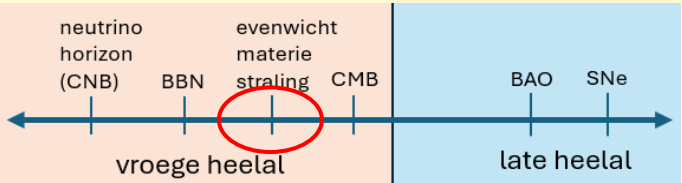


Straling dominantie

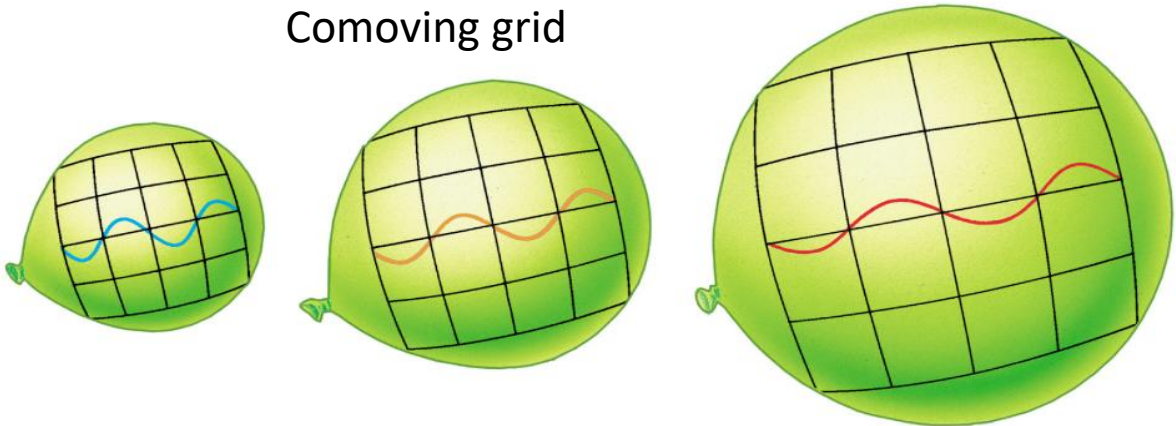
Verdichtingen trekken nog niet (goed) samen

Materie dominantie

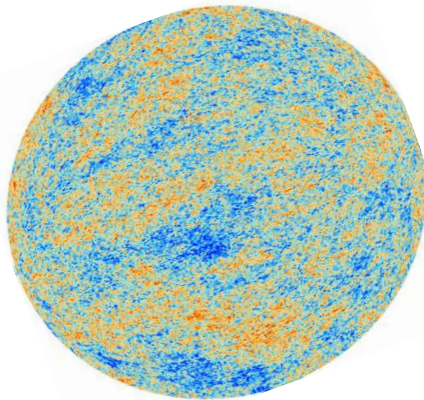
Verdichtingen trekken wel samen door zelf gravitatie



Comoving grid



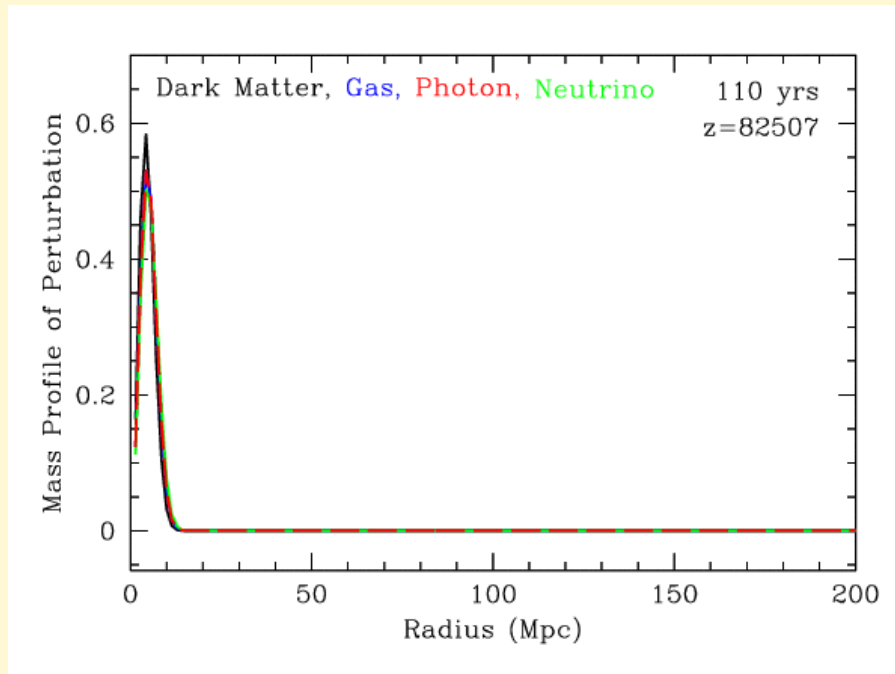
Ballon metafoor met sinaasappelhuid (dichtheidsfluctuaties)



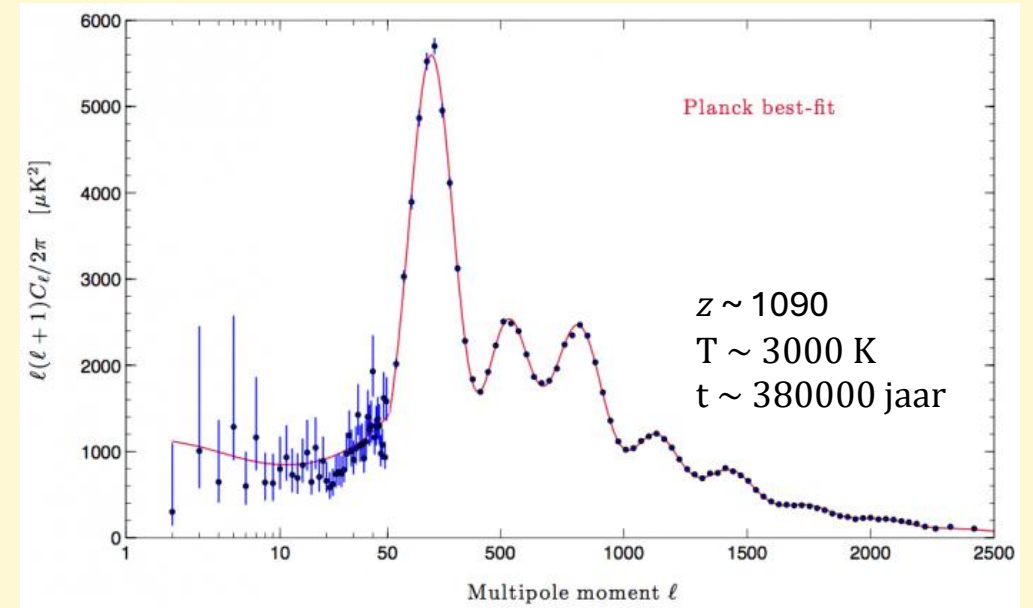
CMB sound horizon

Fotonen slepen (drag) de baryonen mee
→ geluidsgolf (**massa**)

Massa profiel

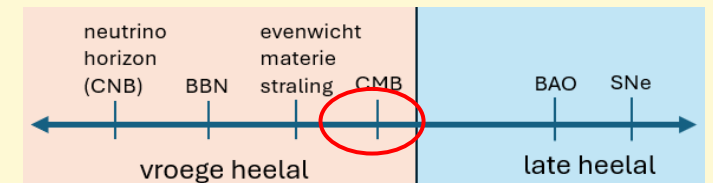


CMB temperature power spectrum



Baryonen volgen ook de donkere materie
→ Samentrekken → verhitting → tegendruk →
afkoeling → weer samen trekken etc. → oscillatie.

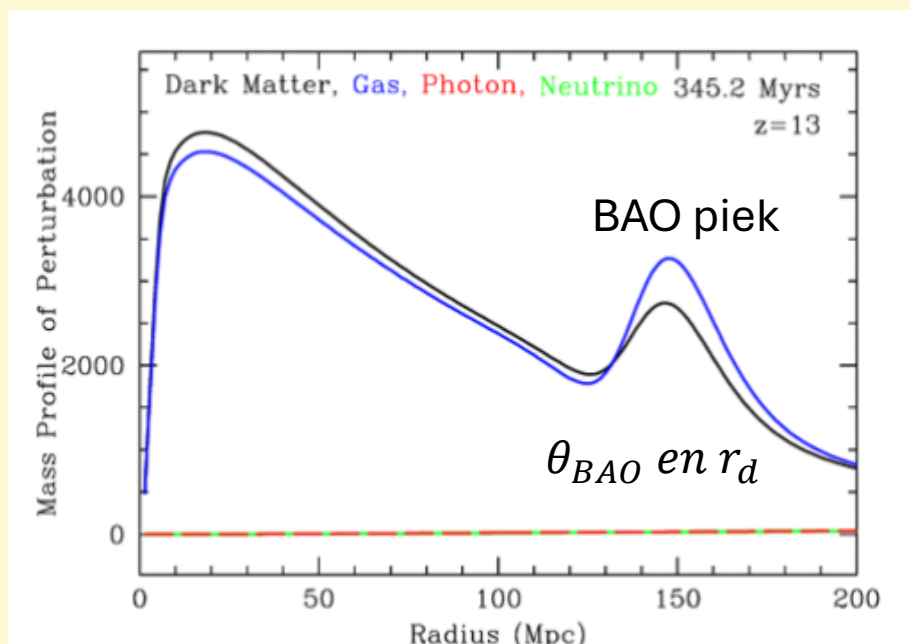
Temperatuur verschillen terug te zien bij de fotonen



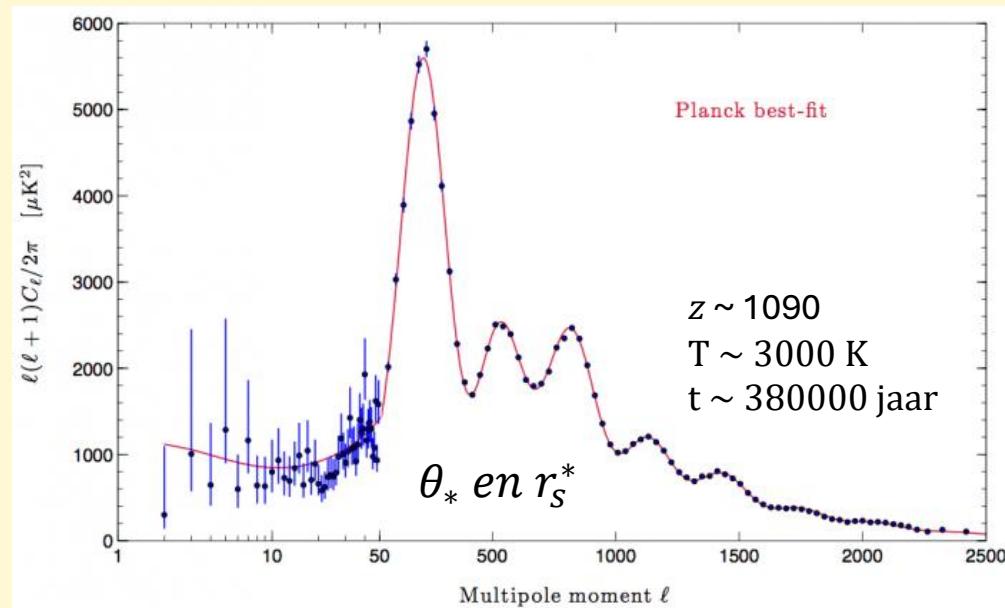
CMB geluidshorizon

Fotonen slepen (drag) de baryonen mee
→ geluidsgolf (**massa**)

Massa profiel

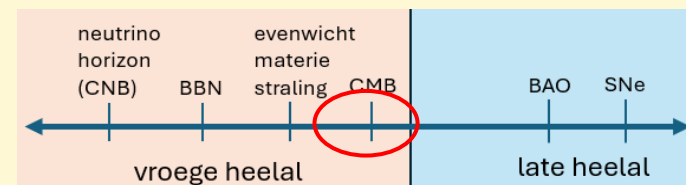


CMB temperature power spectrum



Baryonen volgen ook de donkere materie
→ Samentrekken → verhitting → tegendruk →
afkoeling → weer samen trekken etc. → oscillatie.

Temperatuur verschillen terug te zien bij de fotonen



Geluidshorizon berekenen bij recombinitie (r_s^*) en drag (r_d)

$$r_s^*(z_*) = \int_{z_*}^{\infty} \frac{c_s(z)}{H(z)} dz \quad z \sim 1090, r_s^* \sim 144 \text{ Mpc}$$

Is niet afhankelijk van H_0 , alleen van de energiedichtheden zelf (materie en straling)

$$r_d(z_d) = \int_{z_d}^{\infty} \frac{c_s(z)}{H(z)} dz \quad z \sim 1060, r_d \sim 147 \text{ Mpc}$$

Geluidssnelheid in baryon/fotonen plasma

$$c_s(z) = \frac{c}{\sqrt{3(1 + R(z))}} \quad R(z) = \frac{3\rho_b}{4\rho_\gamma} = \frac{3\Omega_{b,0}h^2}{4\Omega_{\gamma,0}h^2(z+1)}$$

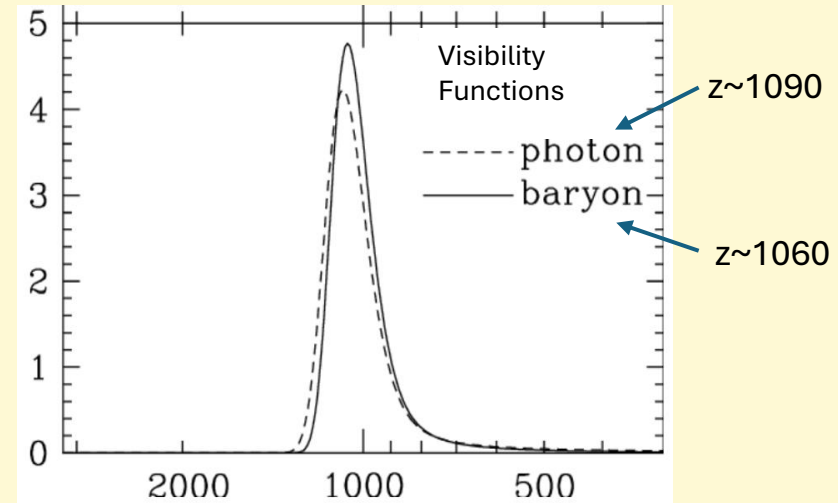
[Cosmology Lecture 19 - AstroBaki](#)

$$H(z) = H_0 E(z)$$

$$E(z) = \sqrt{\Omega_{rel,0}(1+z)^4 + \Omega_{m,0}(1+z)^3 + \Omega_{\Lambda,0}}$$

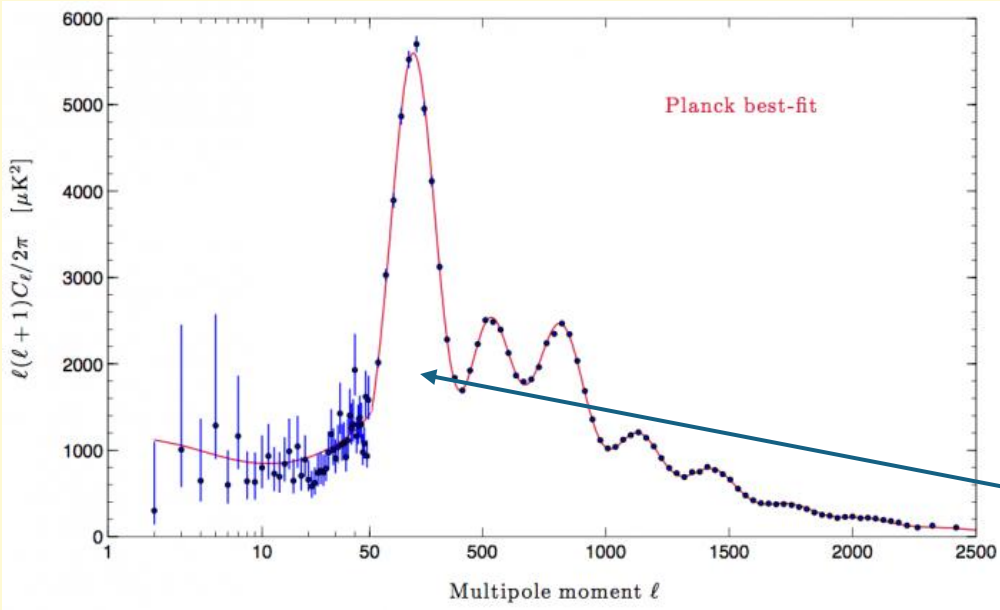
$$H(z) = \sqrt{\Omega_{rel,0}h^2(1+z)^4 + \Omega_{m,0}h^2(1+z)^3}$$

Vroege heelal



roodverschuiving z

Resultaten CMB temperatuur power spectrum (totale materiedichtheid)



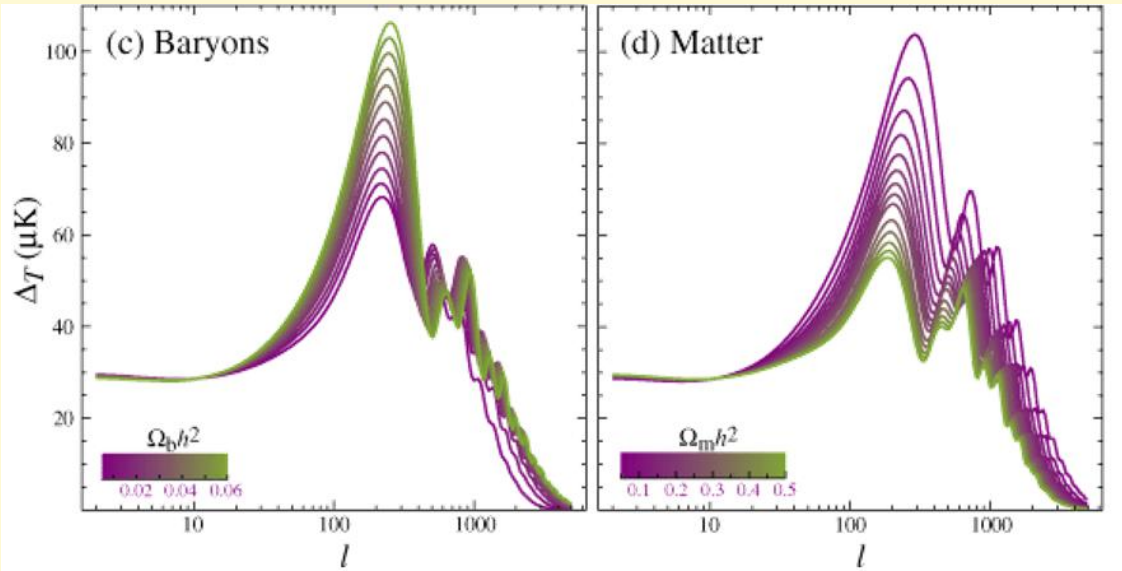
Parameter	Plik best fit
$\Omega_b h^2$	0.022383
$\Omega_c h^2$	0.12011
$100\theta_*$	1.041085
τ	0.0543
$\ln(10^{10} A_s)$	3.0448
n_s	0.96605

$\Omega_{m,0} h^2 = \Omega_{b,0} h^2 + \Omega_{c,0} h^2 = 0.1425$

$\theta_* = \frac{r_s^*(z_*)}{D_M(z_*)}$

vroeghe heelal

late heelal



Verhouding pieken geven info over $\Omega_{b,0} h^2$ & $\Omega_{c,0} h^2$

$D_M(z_*) = \frac{c}{H_0} \int_0^{z_*} \frac{dz}{E(z)}$ Comoving angular diameter distance (transverse)

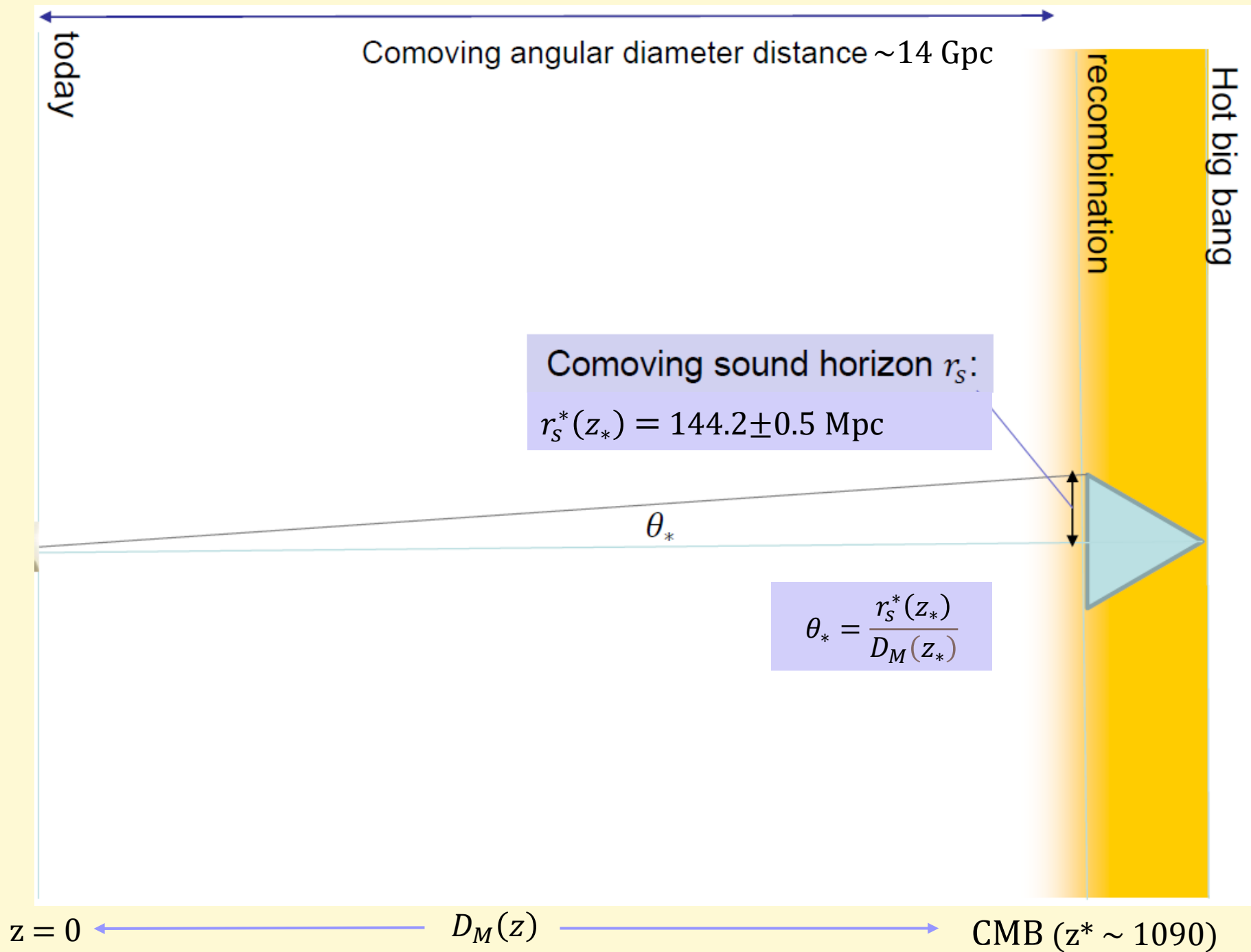
$E(z) = \sqrt{\cancel{\Omega_{rel,0}(1+z)^4} + \Omega_{m,0}(1+z)^3 + \Omega_{\Lambda,0}} \Rightarrow \sqrt{\Omega_{m,0}(1+z)^3 + 1 - \Omega_{m,0}}$

late heelal

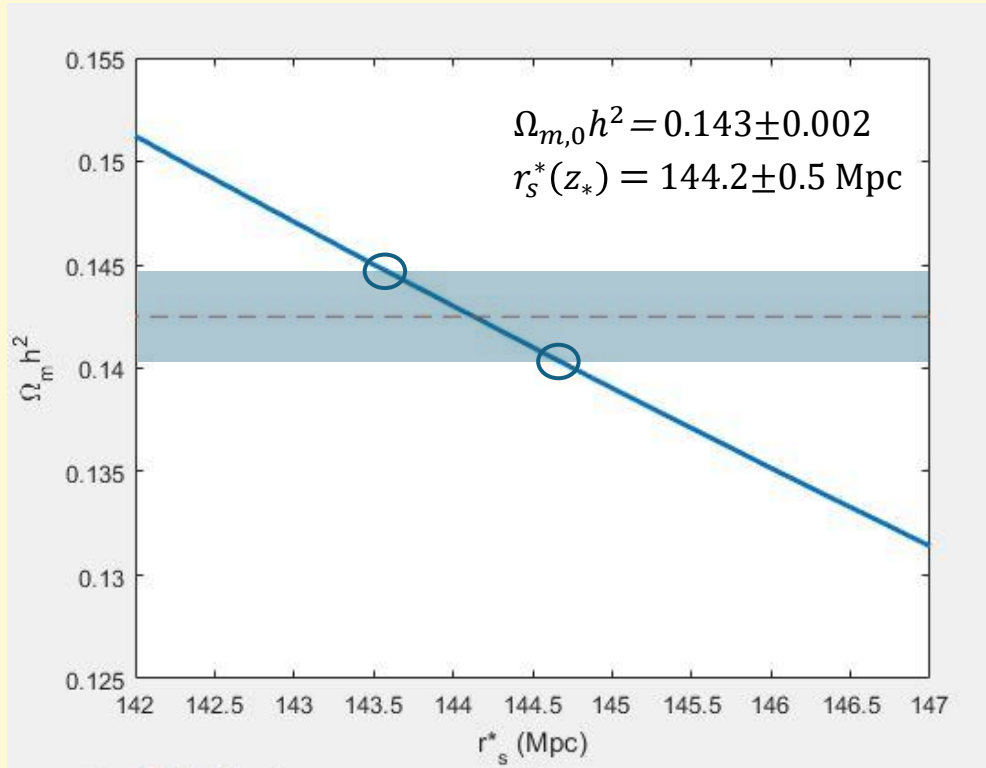
$\Omega_{\Lambda,0} = 1 - \Omega_{m,0}$
vlak heelal

$z_* = 1090$, dus best een lang stuk evolutie in $D_M(z_*)$

r_s als spil



Afleiding H0 uit CMB resultaten

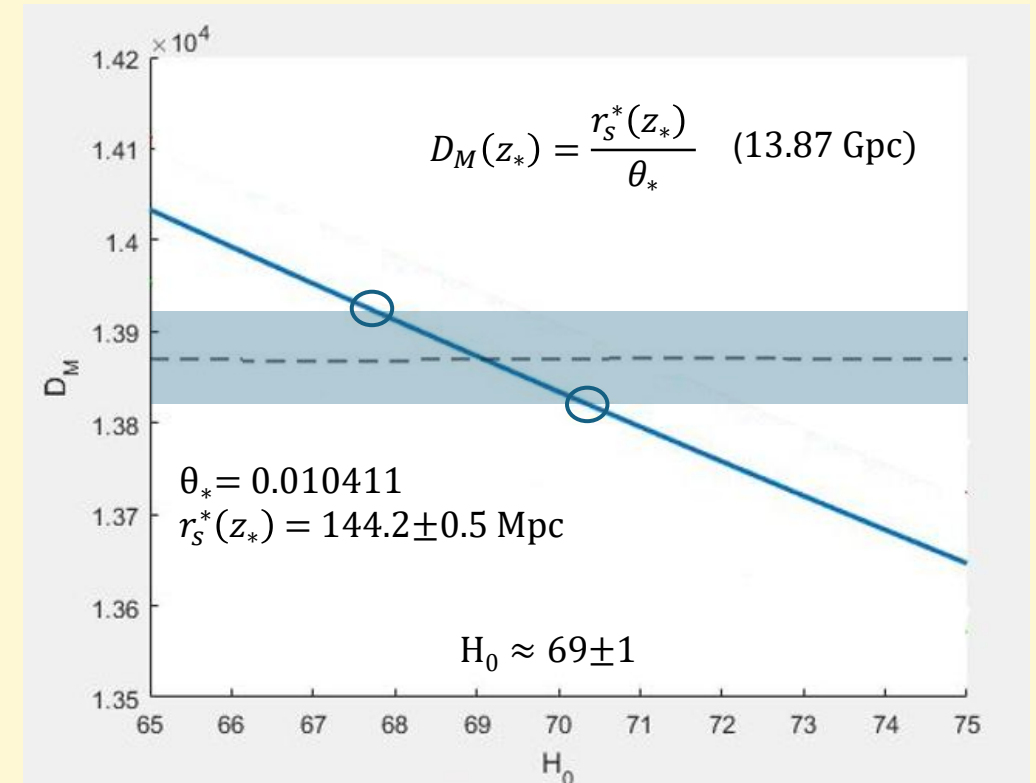


$$D_M(z_*) = \frac{r_s^*(z_*)}{\theta_*}$$

late heelal

$$D_M(z_*) = c \int_0^{z_*} \frac{dz}{H(z)} \quad H_0 = 100h$$

$$H(z) = \sqrt{\Omega_{m,0} h^2 (z+1)^3 + h^2 - \Omega_{m,0} h^2}$$



$$r_s^*(z_*) = \int_{z_*}^{\infty} \frac{c_s(z)}{H(z)} dz$$

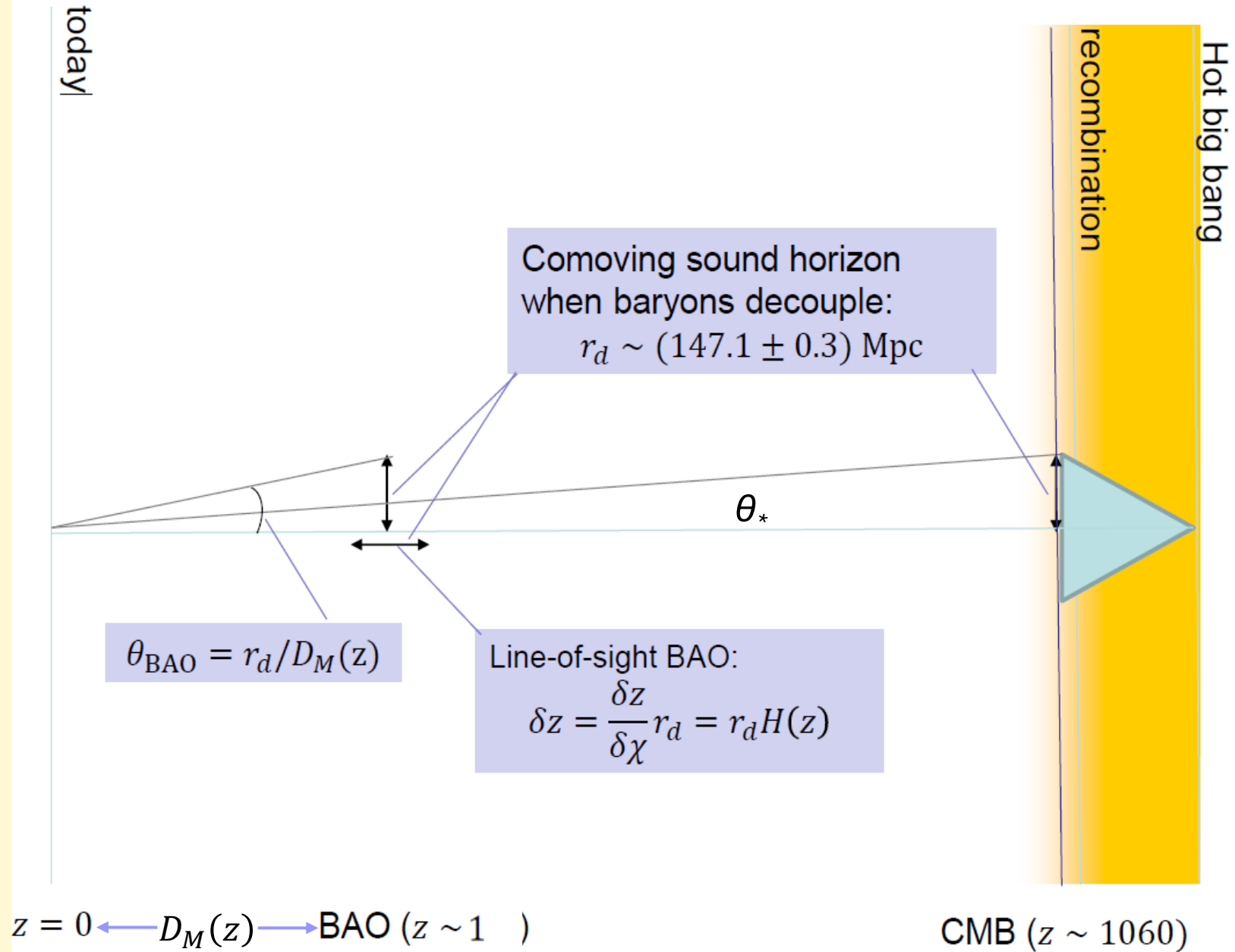
vroege heelal

$$H(z) = \sqrt{\Omega_{\text{rel},0} h^2 (z+1)^4 + \Omega_{m,0} h^2 (z+1)^3}$$

$\Omega_{m,0} h^2$ is hier de cruciale parameter en ook het minst 'betrouwbaar' bekend

$z_* = 1090$, dus best een lang stuk evolutie in $D_M(z)$

CMB and BAO consistency in Λ CDM



BAO pieken in late heelal

BAO piek (in het late heelal)

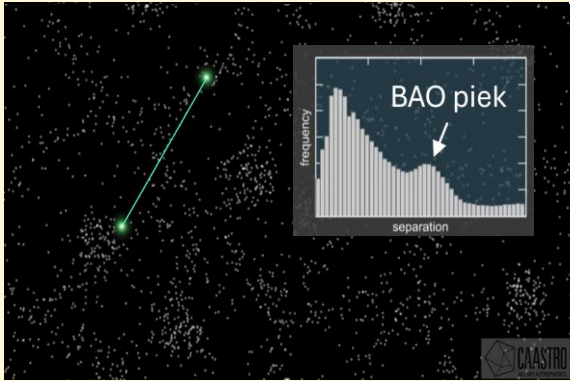
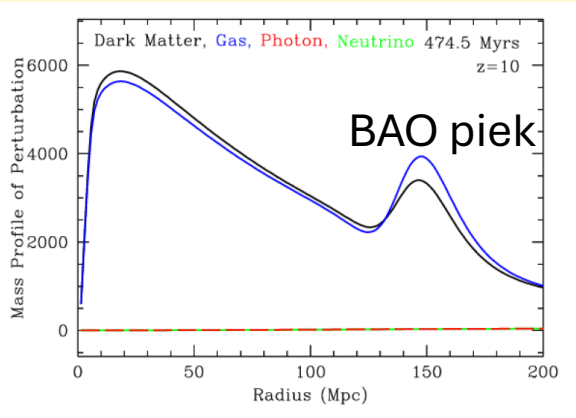
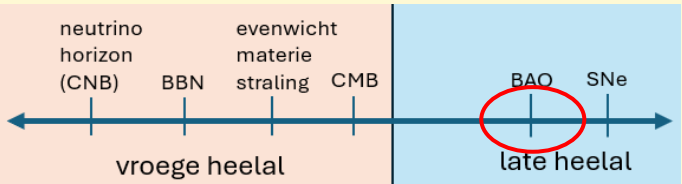
$$\theta_{BAO} = \frac{r_d(z_d)}{D_M(z_{BAO})}$$

Comoving distance (transverse, flat universe)

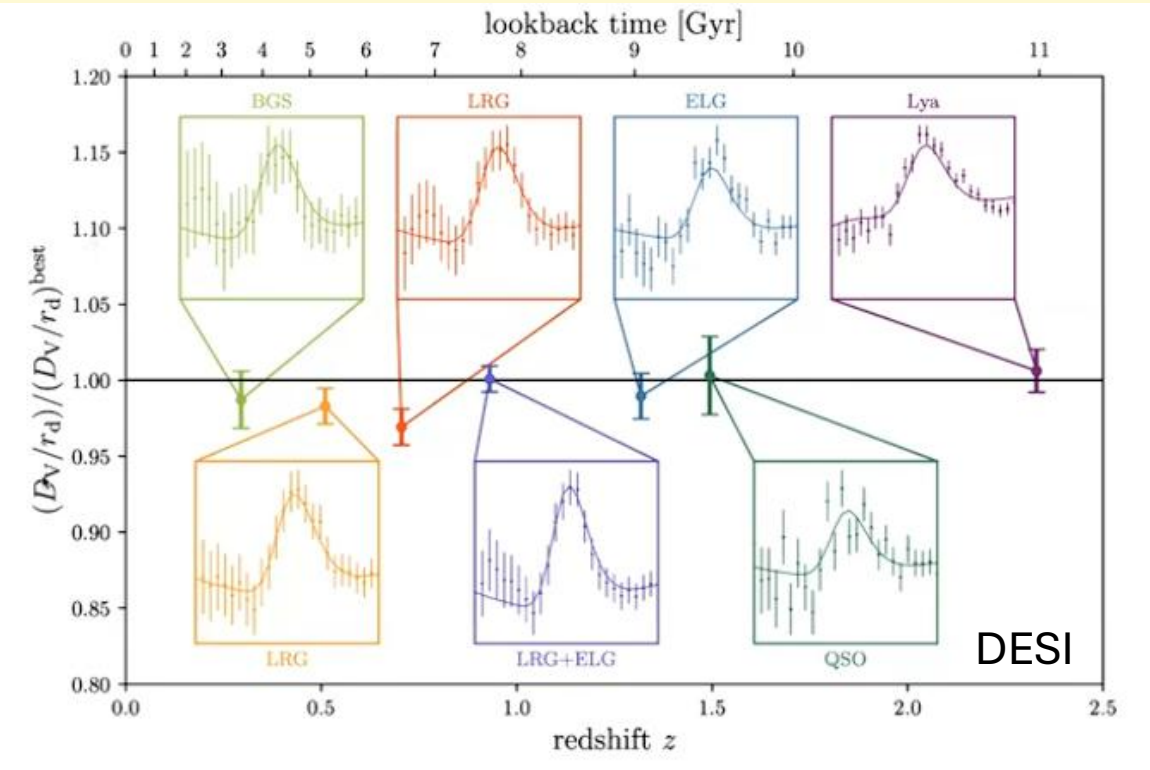
$$D_M(z_{BAO}) = \frac{c}{H_0} \int_0^{z_{BAO}} \frac{dz}{E(z)}$$

$$E(z) = \sqrt{\Omega_{m,0}(z + 1)^3 + 1 - \Omega_{m,0}}$$

z~1, dus een klein stuk evolutie bij D_M



Correlation function (astronomy) - Wikipedia



Verschillende z → meer controle

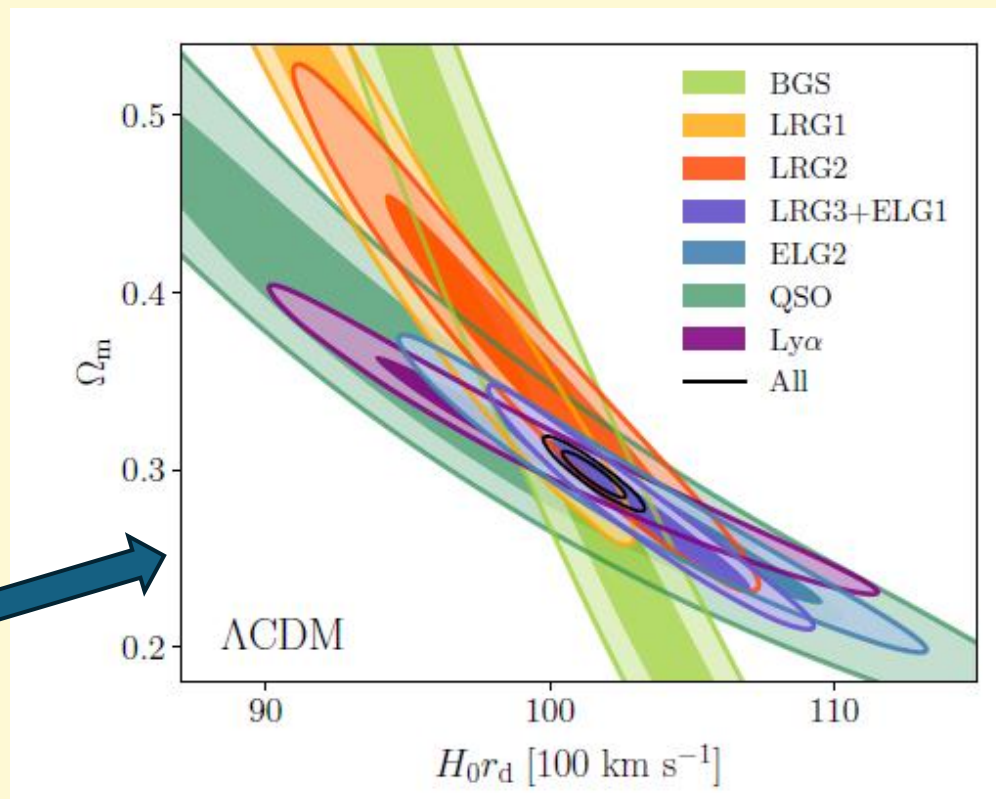
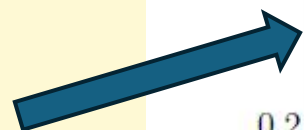
Degeneracy $H_0 r_d$ en Ω_m – (afhankelijkheid van Ω_m)

$$\theta_{BAO} = \frac{r_d(z_d)}{D_M(z_{BAO})}$$



$$H_0 r_d = \theta_{BAO} \int_0^{z_{BAO}} \frac{dz}{E(z)}$$

$$E(z) = \sqrt{\Omega_{m,0}(z+1)^3 + 1 - \Omega_{m,0}}$$



Setjes $\{\theta_{BAO}, z_{BAO}\}$ gemeten $\rightarrow$ diverse curven $\{H_0 r_d, \Omega_{m,0}\}$

Snijpunt $\rightarrow$

$$\left. \begin{array}{l} \Omega_m = 0.2975 \pm 0.0086, \\ h r_d = (101.54 \pm 0.73) \text{ Mpc}, \end{array} \right\} \text{ DESI DR2}$$

Onafhankelijk van CMB parameters $\theta_*, \Omega_{c,0} h^2$ en $\Omega_{b,0} h^2$

gemeten

$$\frac{H_0 r_d(z_d)}{r_d} = \frac{102 \times 100}{147} \sim 69 \text{ km/s/Mpc}$$

berekend

Samenvattend

De evolutie van het heelal wordt gedreven door de volgende *energiedichtheden*

- Fotonen (Ω_γ)
- Neutrino's in vaste verhouding tot de fotonen (Ω_ν)
- De baryonen (gewone materie) (Ω_b)
- Donkere materie (Ω_c)
- De rest is donkere energie in een vlak heelal (Ω_Λ)

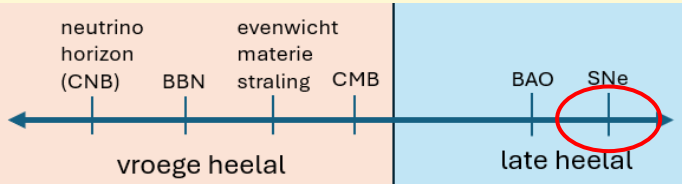
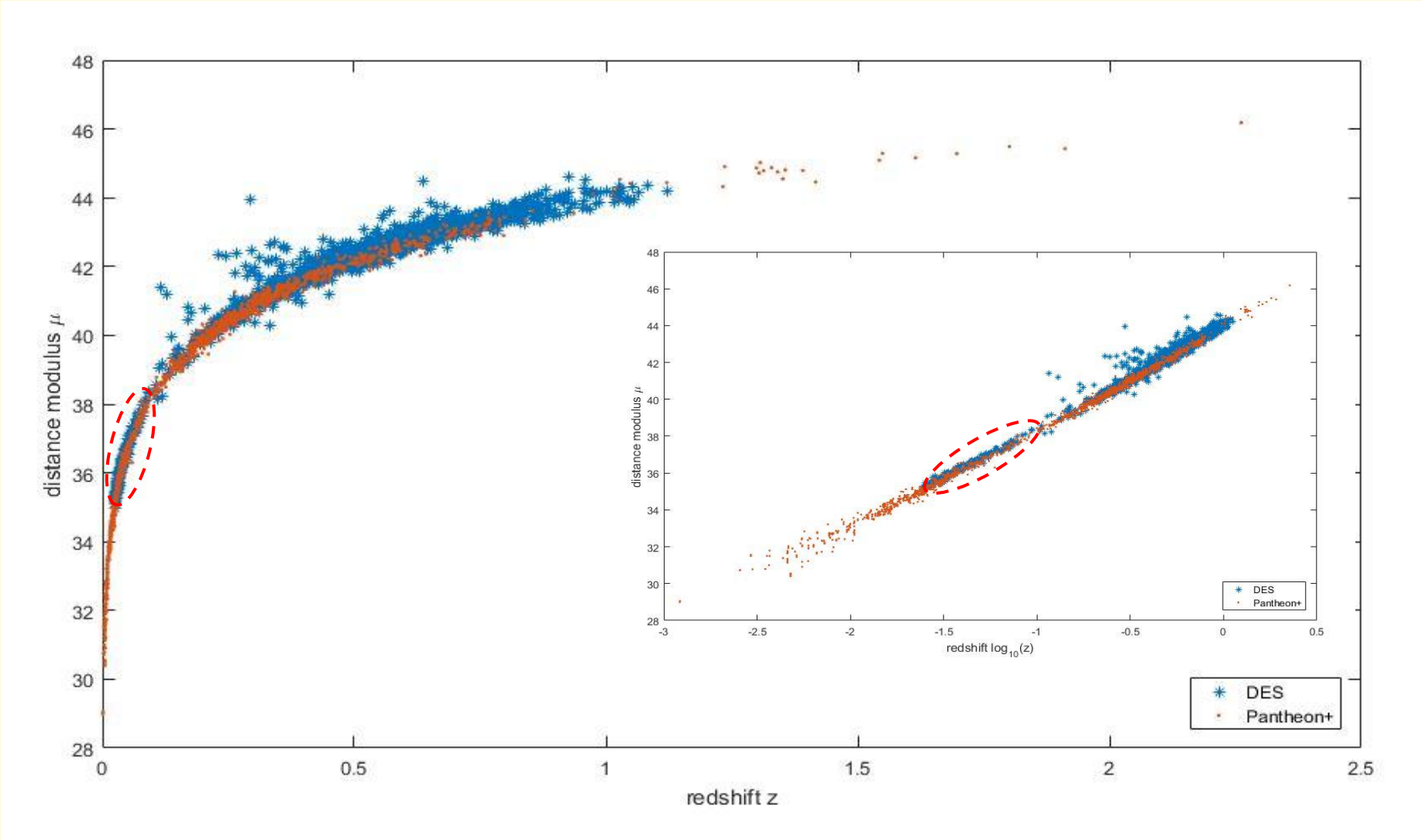
Er is een *ankerpunt* dat we kunnen berekenen en meten: de sound horizon (geluidshorizon) n.a.v. de geluidsgolf van baryonen.

- M.b.v. fotonen bij de CMB (iets hogere temperatuur in de geluidsgolf)
- M.b.v. baryonen (en indirect de donkere materie) de booggolf van de baryonen weerspiegeld in de distributie van sterrenstelsels (BAO)

Dit geeft een tempo van uitdijng weerspiegeld in de *Hubble constante* $< 70 \text{ Mpc/km/s}$ ($H_0 \sim 67-69$)

Nu lokaal uitdijing meten

High redshift Hubble diagram samples (Pantheon+ en DES)



High redshift Hubble diagram (theorie)

Distance modulus

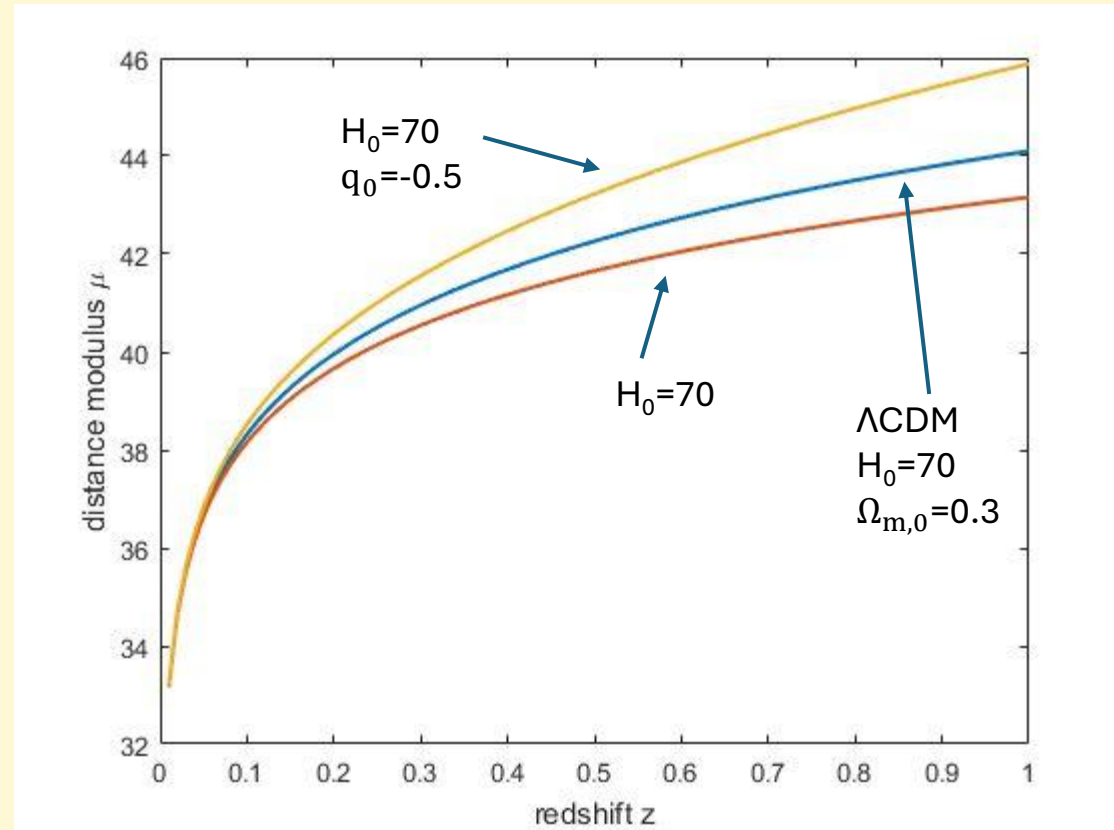
$$S = \frac{L}{4\pi d_L^2}$$

$$\mu_0 = m - M_B = 5 \log \left(\frac{d_L(z)}{\text{Mpc}} \right) + 25$$

Λ CDM model

$$d_L(z) = (1+z) \frac{c}{H_0} \int_0^z \frac{dz'}{E(z')}$$

$$E(z) = \sqrt{\Omega_{m,0}(z+1)^3 + 1 - \Omega_{m,0}}$$

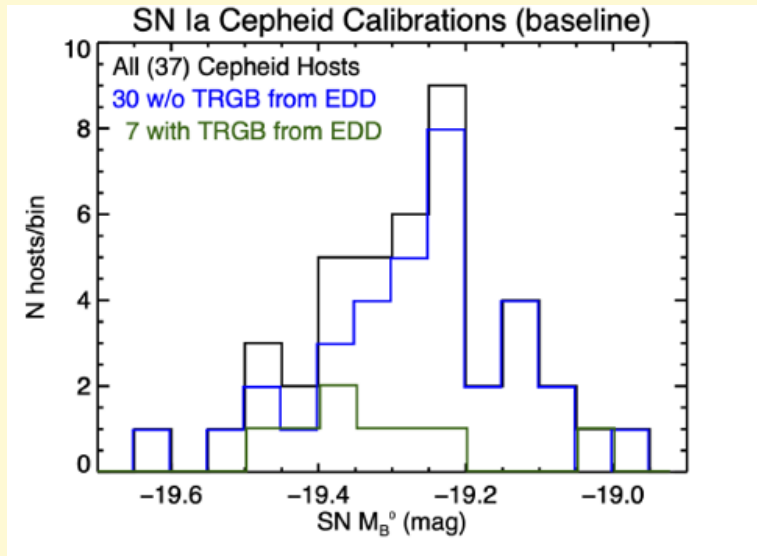


Cosmography – Taylor reeks

$$d_L(z) = \frac{c}{H_0} \left(z + \frac{1}{2} (1 - q_0) z^2 + O(z^3) + \dots \right) \quad \text{als } z \rightarrow 0 \quad d_L(z) = \frac{cz}{H_0} \quad (v=H_0 * r)$$

$$q_0 = \frac{3}{2} \Omega_{m,0} - 1$$

Calibration with the distance ladder (Cepheids)



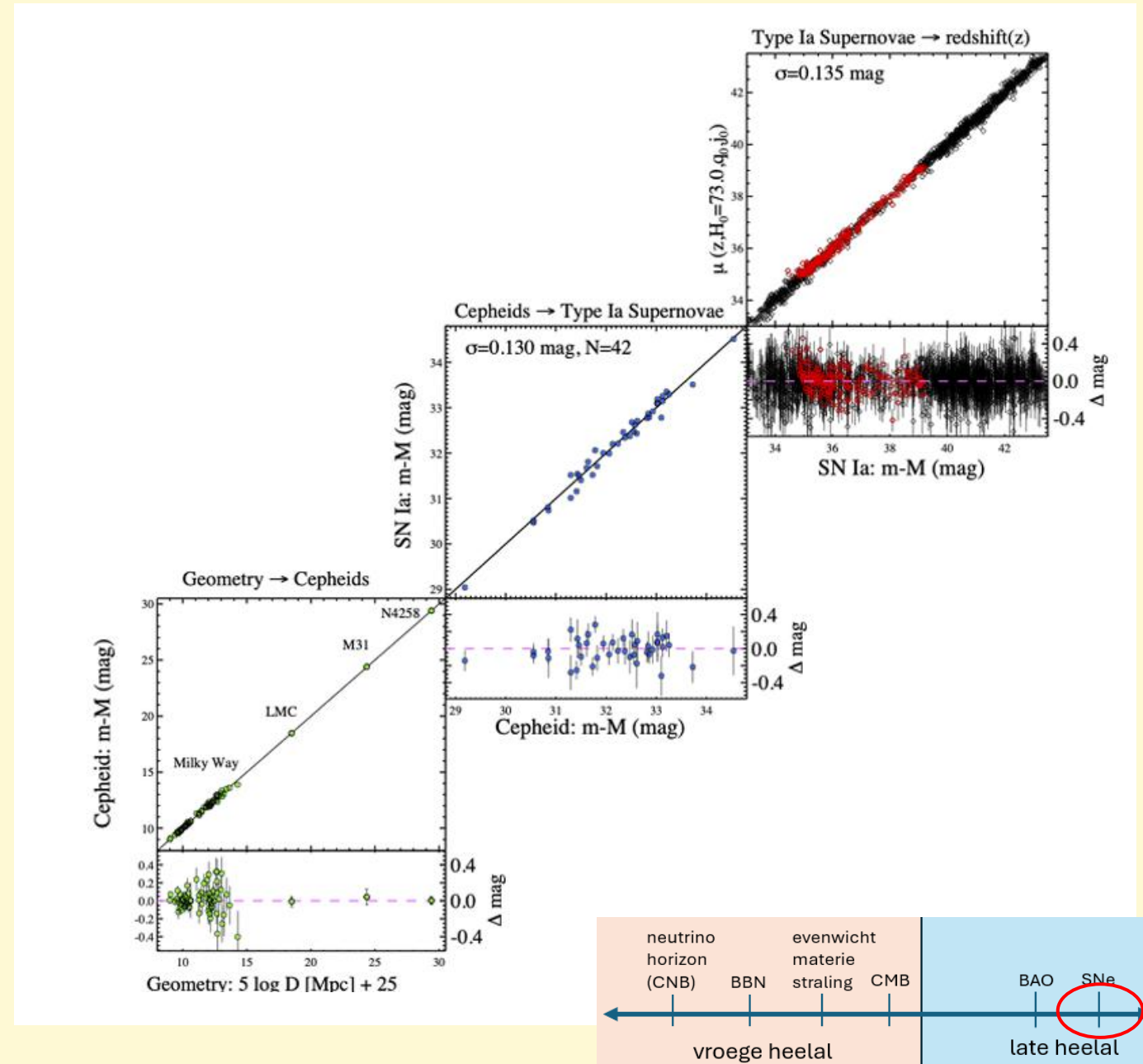
$$M_B^0 = -19.253 \pm 0.027 \text{ mag}$$

$$H_0 = 73.04 \pm 1.01 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

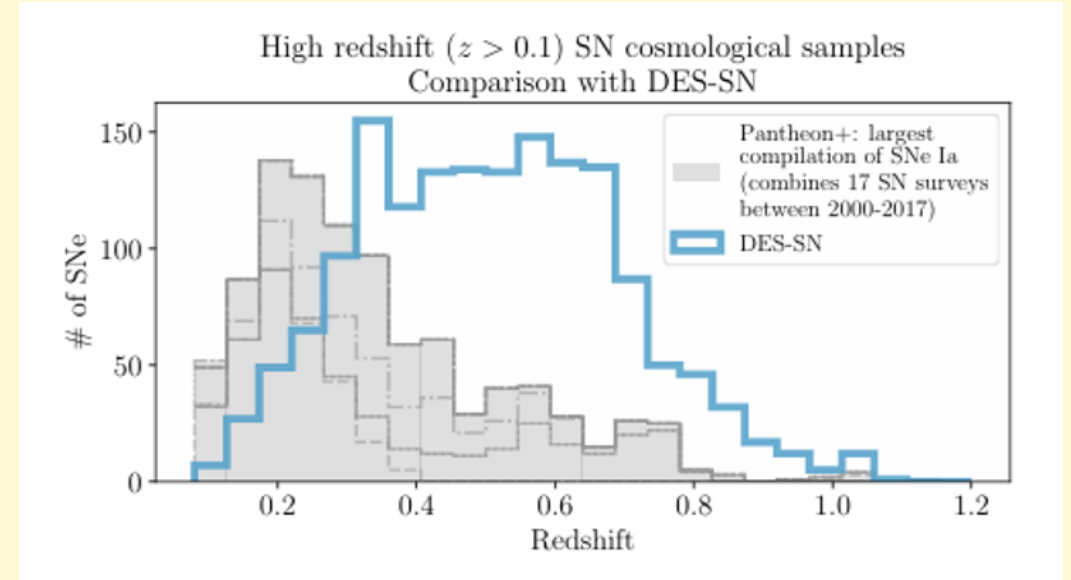
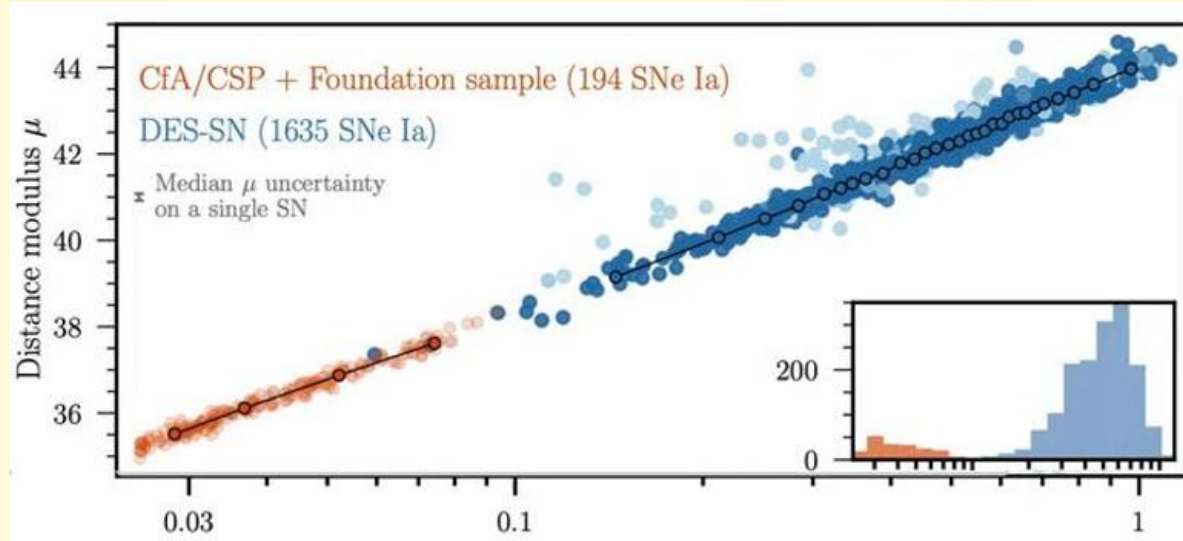
$$0.03 \text{ mag or } 1 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

$$q_0 = -0.51 \pm 0.024$$

Riess_2022_2112.04510



Dark energy survey (DES) sample, nadruk op $z > 0.1$, single telescope, single camera



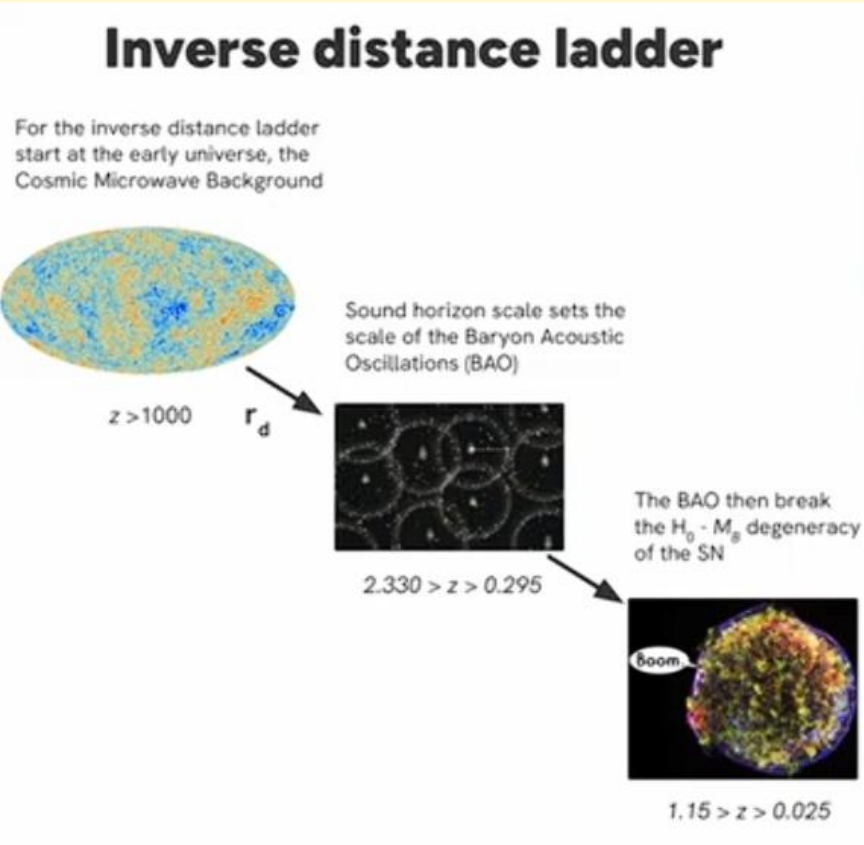
DES is een dieper (meer hogere roodverschuiving) sample dan Pantheon+

DES is waargenomen is diverse specifieke bundels

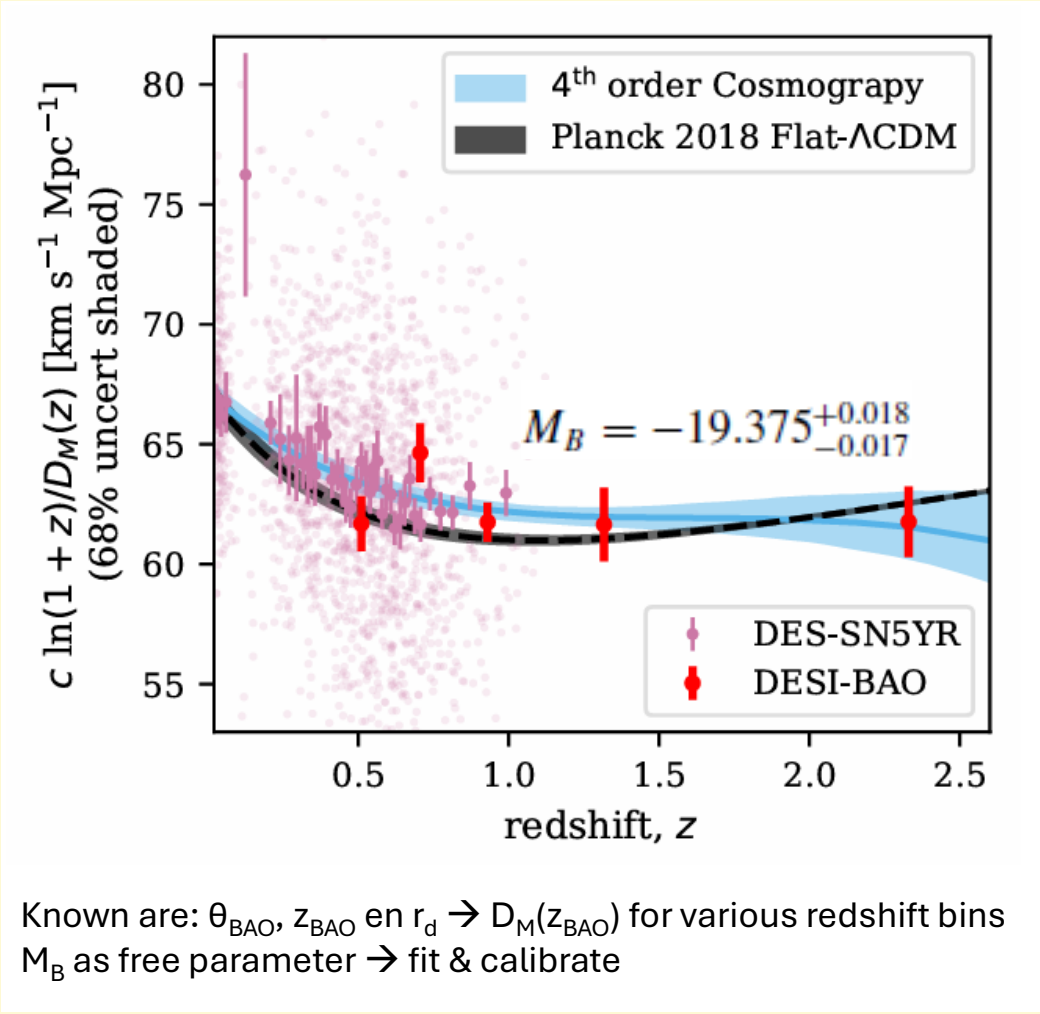


[\[2401.02945\] The Dark Energy Survey Supernova Program: Cosmological Analysis and Systematic Uncertainties](#)

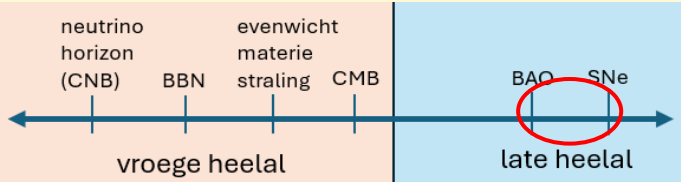
Calibration with the inverse distance ladder



$r_d \rightarrow$ afstand BAO bij $z \rightarrow$ een fit geeft SNe afstand bij waargenomen z van bijbehorende stelsel.
Geen kalibratie met Cepheïden nodig.

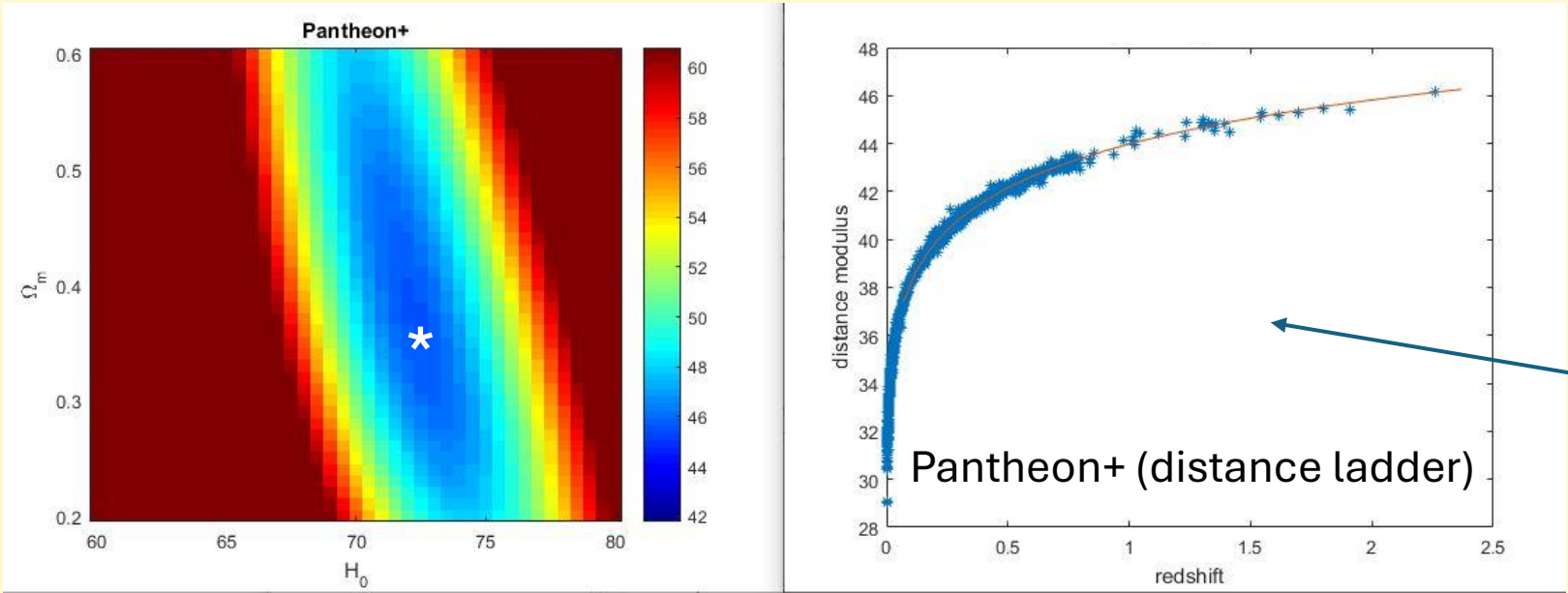


$M_B = -19.375 \longrightarrow H_0 \sim 69 \text{ km s}^{-1} \text{Mpc}^{-1}$



Degeneratie, hubble diagrammen lokaal - distance modulus (Λ CDM model)

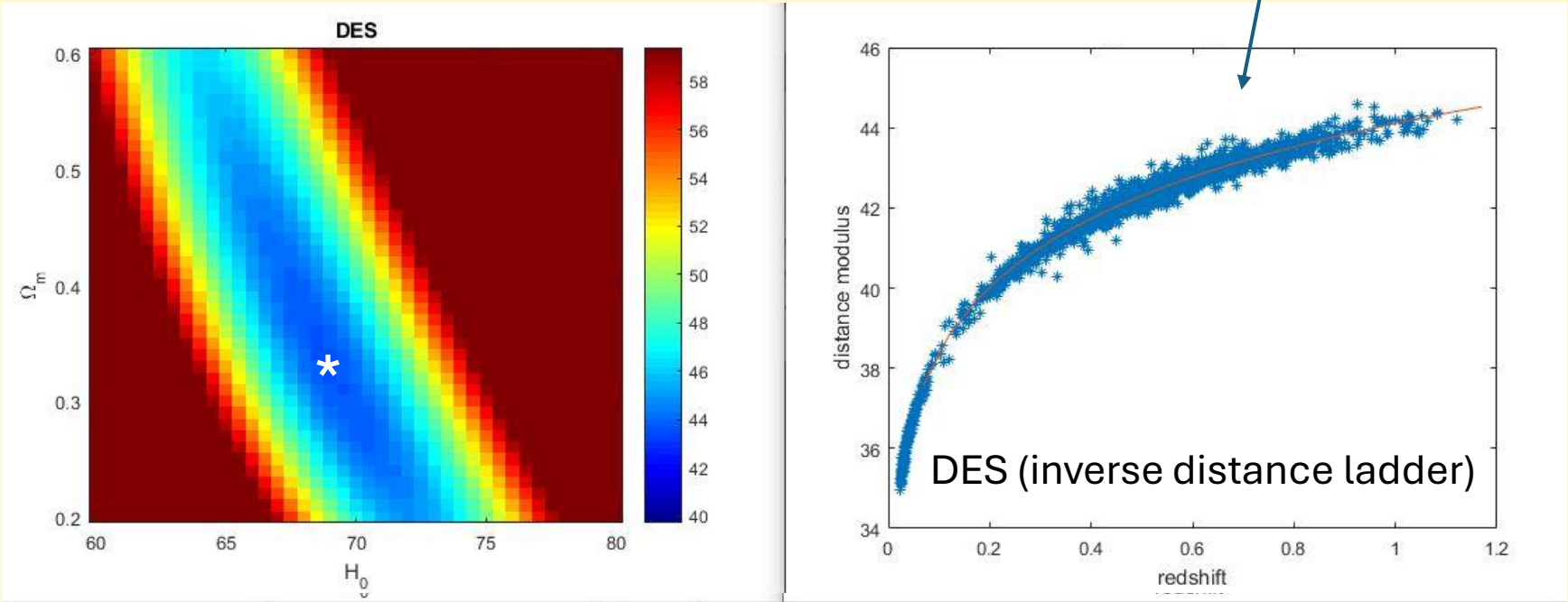
*
 $H_0 = 72$
 $\Omega_{m,0} = 0.36$



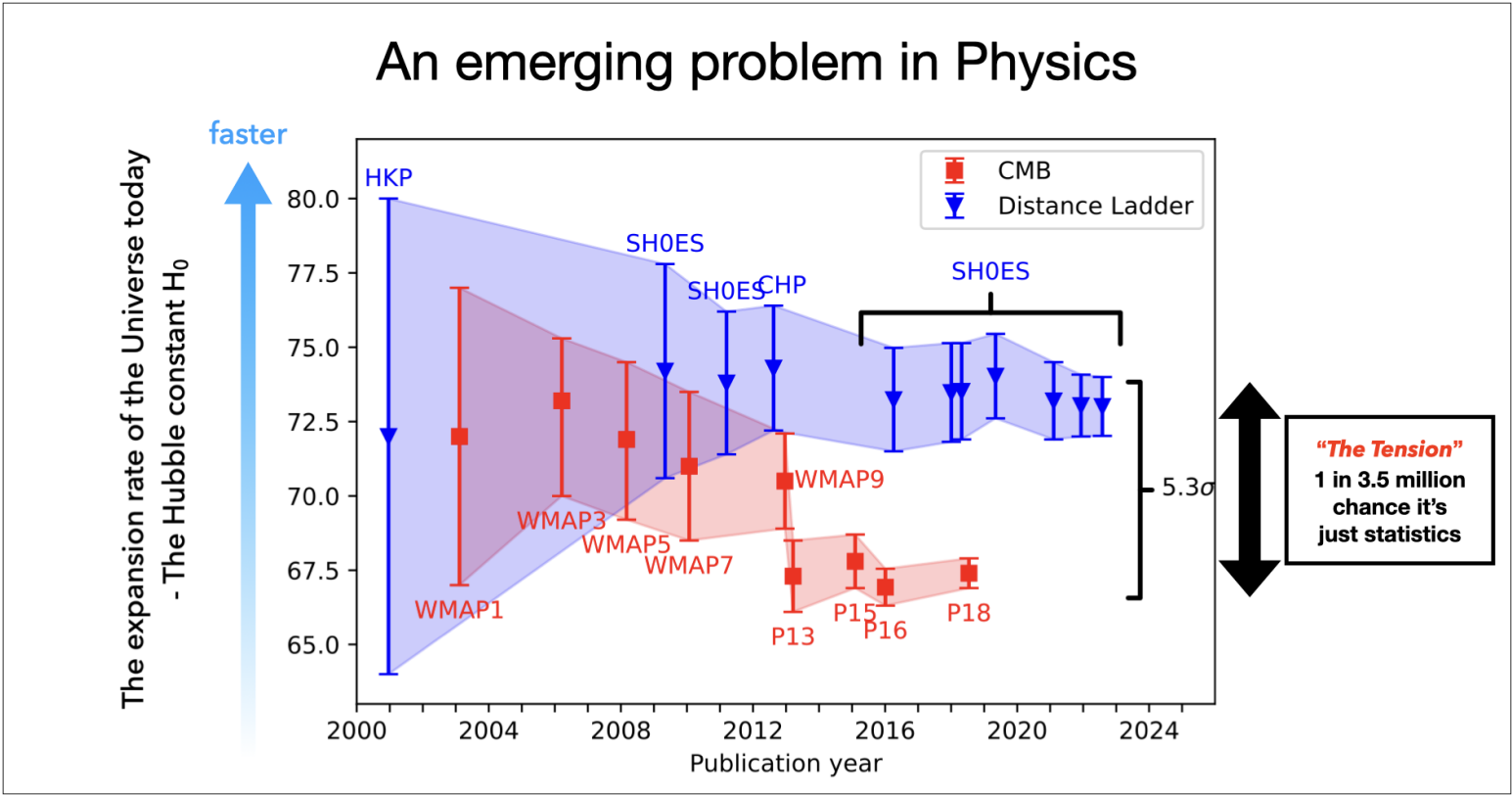
Verschillende kalibraties:

- Cepheiden
- Sound horizon r_d

*
 $H_0 = 69$
 $\Omega_{m,0} = 0.33$

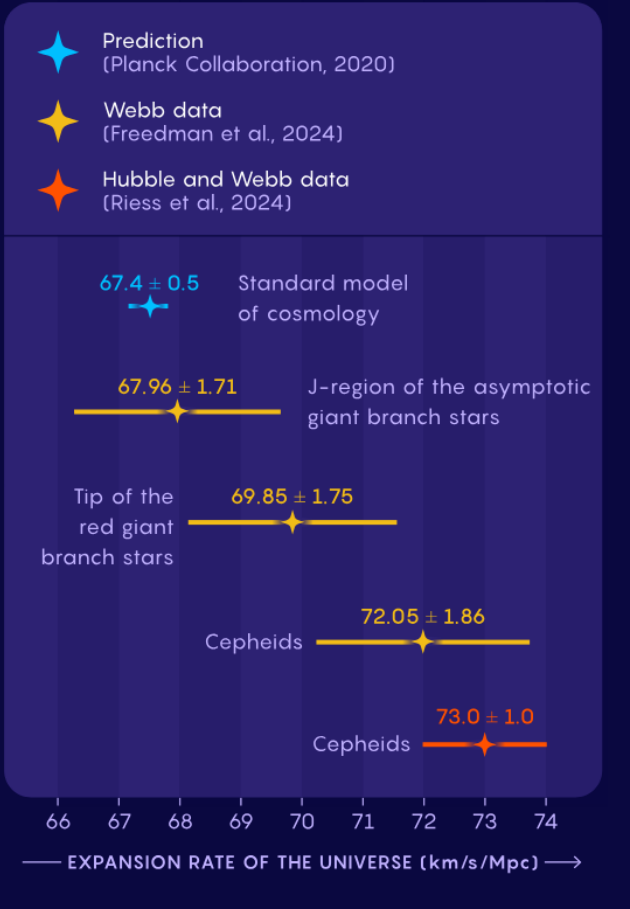


Hubble tension

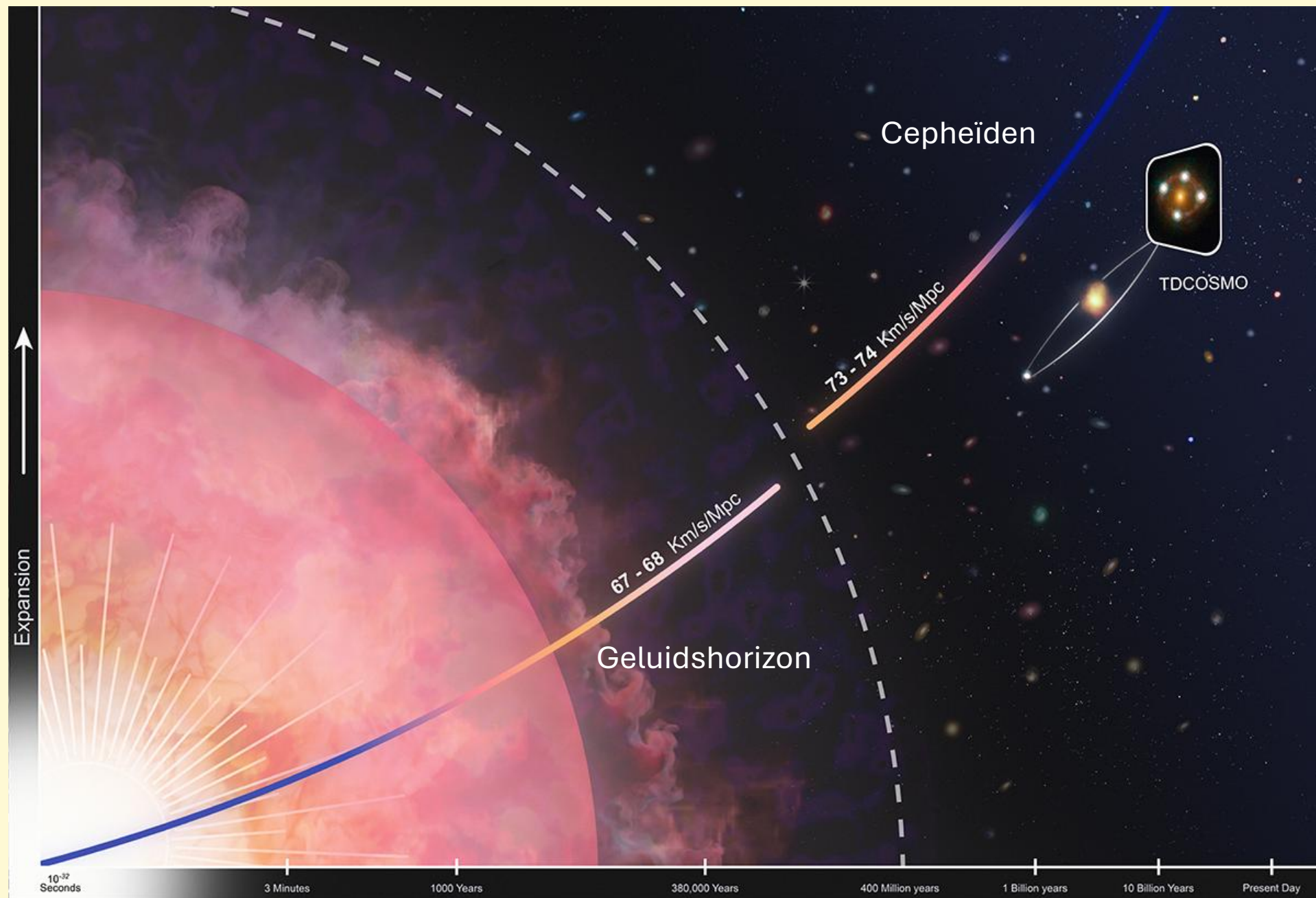


The Hubble Constant Controversy

For years, measurements of the universe's expansion rate have been overshooting the prediction. Despite new data from the James Webb Space Telescope, different methods continue to yield varying results, leaving the true expansion rate uncertain.



Samenvattend



Tot slot

Andere methoden:

- Lensing (quasars, supernovae)
- Zwaartekrachtgolven (merging neutron stars)
- Piek massa power spectrum (matter-radiation equality)

Mogelijke verklaringen verschil:

- Locale afwijkingen van vlak heelal
- Decaying or interacting dark matter
- Early dark energy
- Dynamical dark energy $w_0 w_a$
- Iets anders onderweg ...

Toekomstige waarnemingen:

- DESI
- Euclid
- Vera Rubin telescoop (LSST) Legacy Survey of Space and Time
- Roman Grace space telescope



EINDE